

# Deep Learning, histoire et principes...

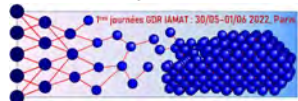
De la régression aux GANs

[Jean-Luc.Parouty@simap.grenoble-inp.fr](mailto:Jean-Luc.Parouty@simap.grenoble-inp.fr)

1<sup>ère</sup> journée

## GDR IAMAT

30 mai – 01 juin 2022, Paris



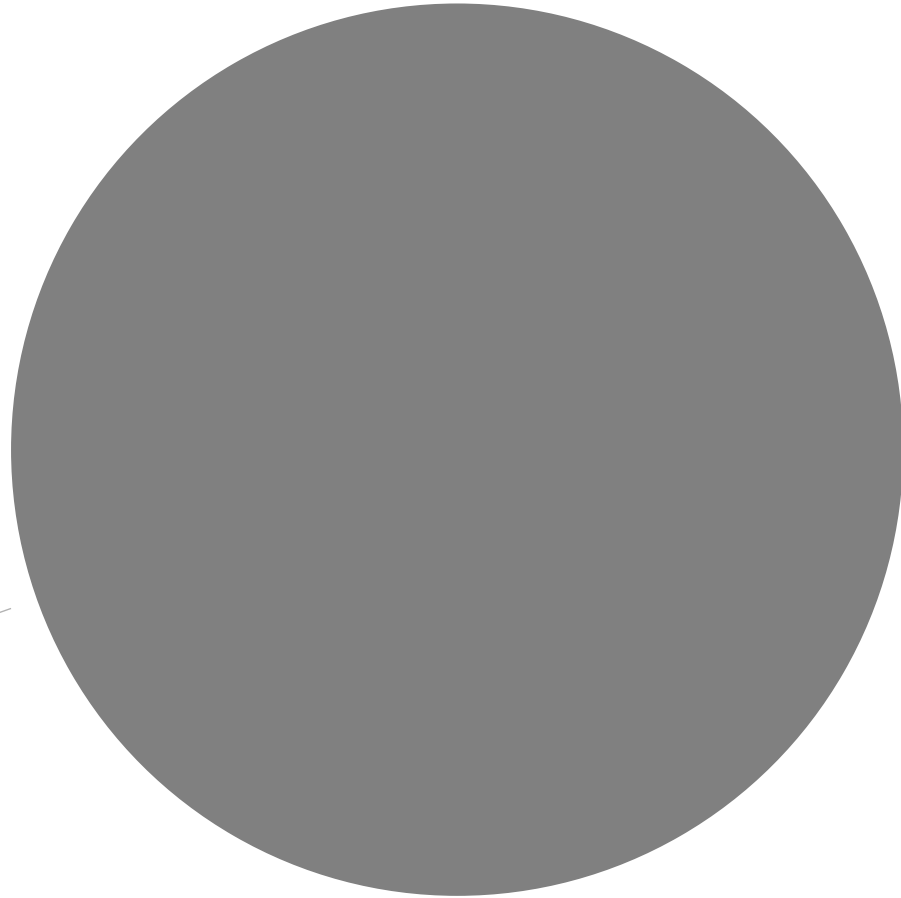


Homer Simpson's brain seen with MRI/X ray.

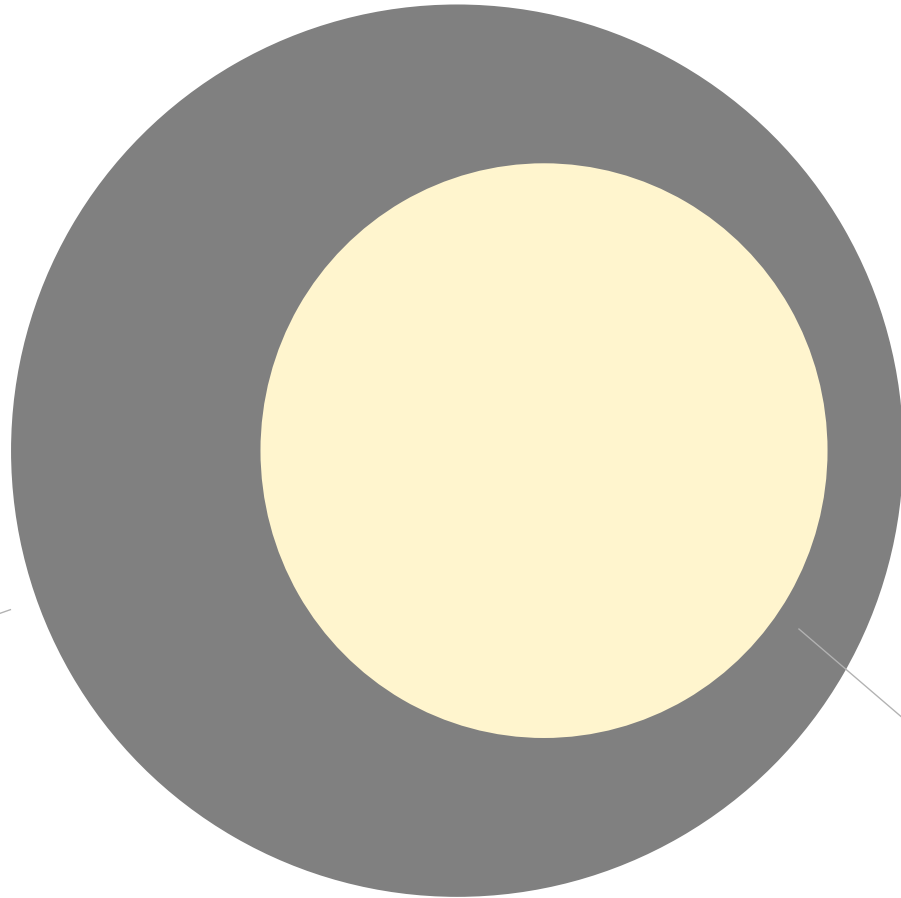
Why would we want to use **artificial intelligence**, when natural intelligence work so well?

- What is an artificial neuron ?
- How did they arrive ?
- How does it work ?

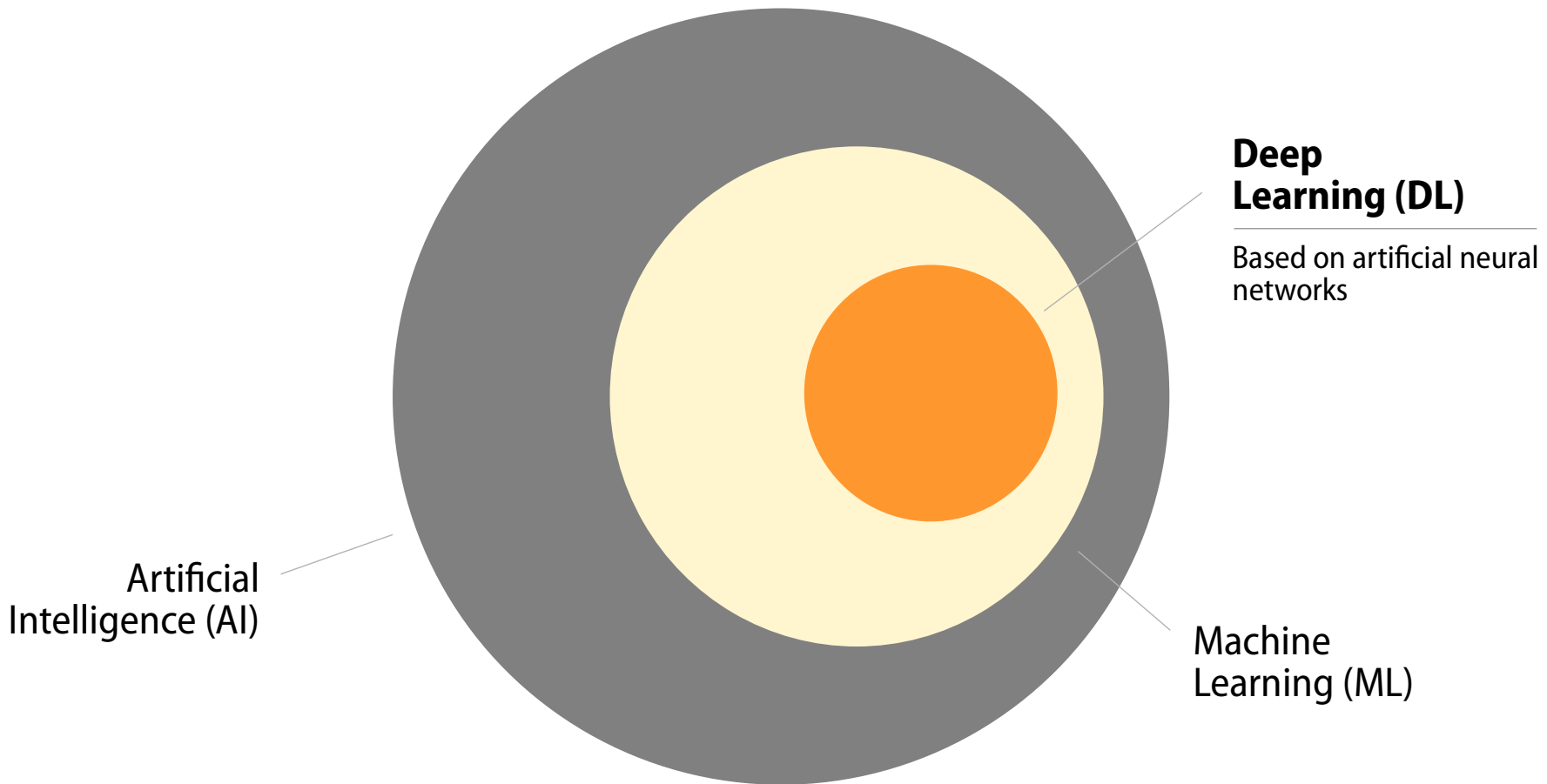
Artificial  
Intelligence (AI)



Artificial  
Intelligence (AI)

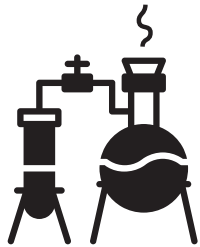


Machine  
Learning (ML)



# Scientific paradigms

1<sup>st</sup> paradigm



Experimental science

2<sup>nd</sup> paradigm

$$i\hbar \frac{d}{dt} |\Psi(t)\rangle = \hat{H} |\Psi(t)\rangle$$

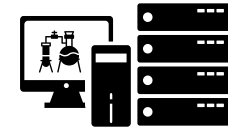
$$\nabla \times H = J + \frac{\partial D}{\partial t}$$

$$F = G \cdot \frac{m_1 \cdot m_2}{r^2}$$

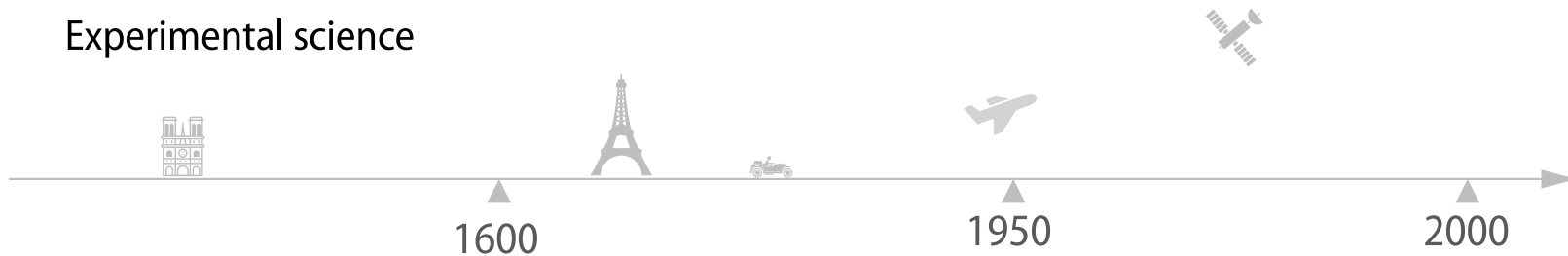
Theoretical science

3<sup>rd</sup> paradigm

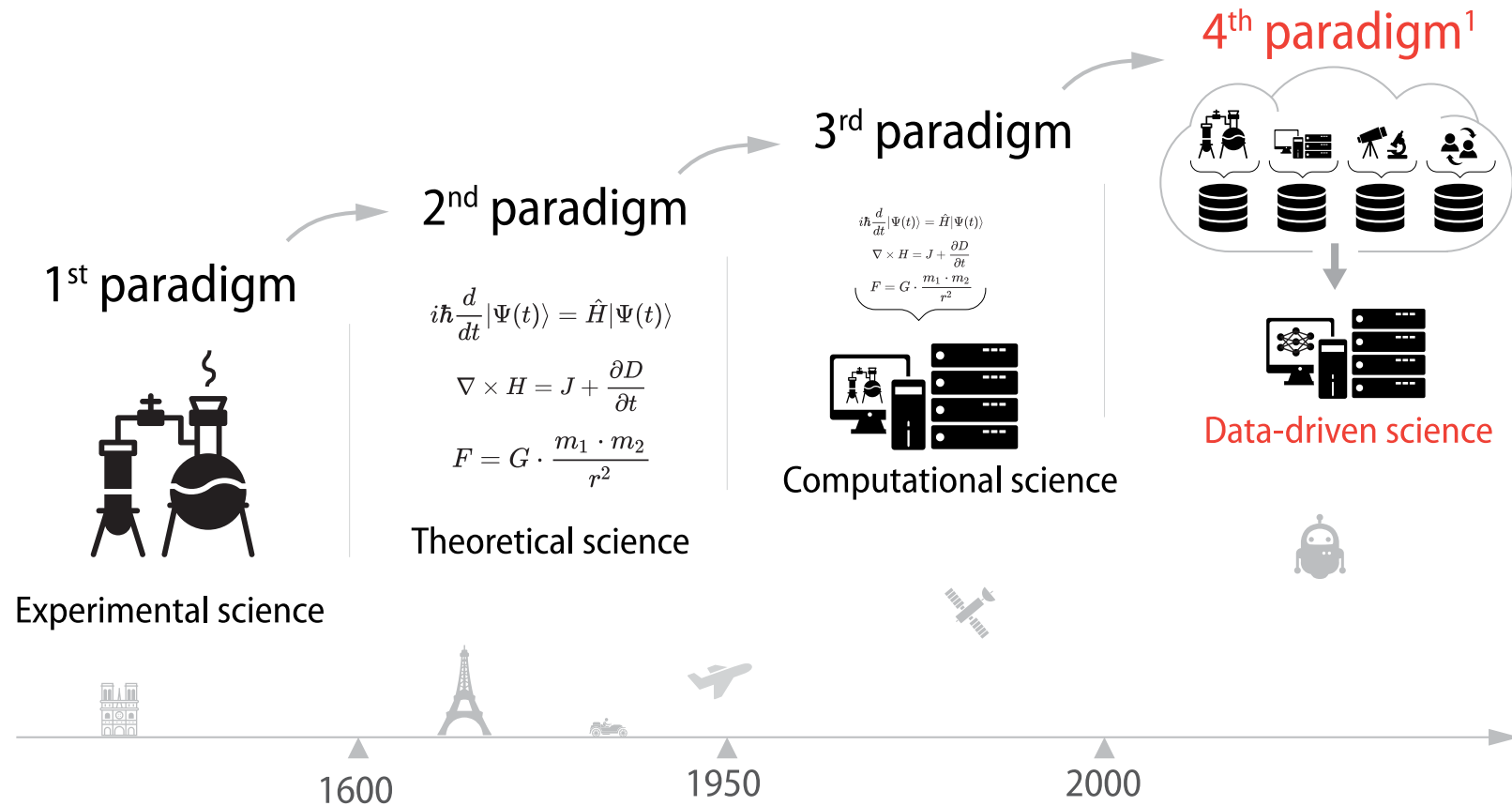
$$i\hbar \frac{d}{dt} |\Psi(t)\rangle = \hat{H} |\Psi(t)\rangle$$
$$\nabla \times H = J + \frac{\partial D}{\partial t}$$
$$F = G \cdot \frac{m_1 \cdot m_2}{r^2}$$



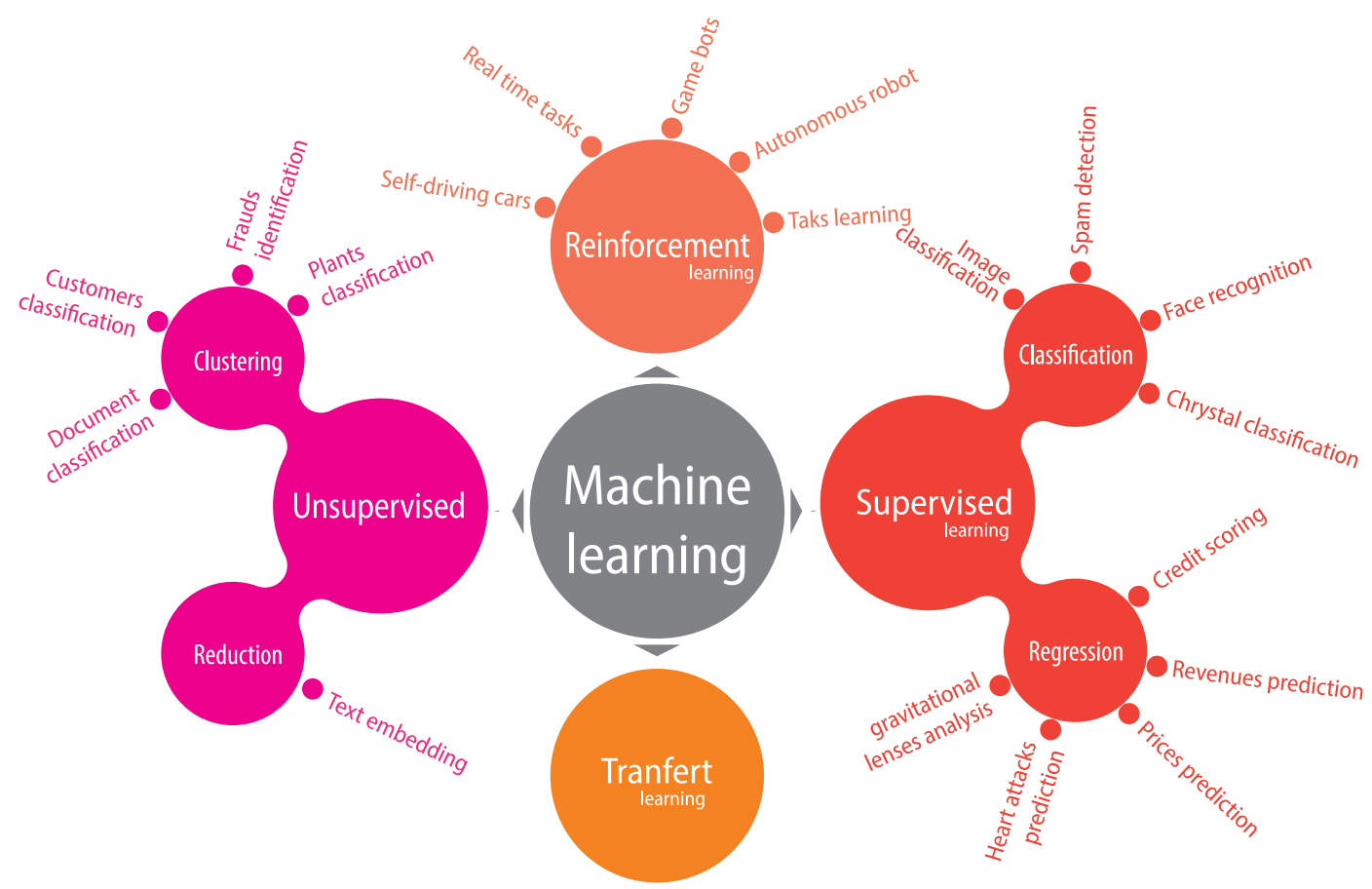
Computational science



# Scientific paradigms

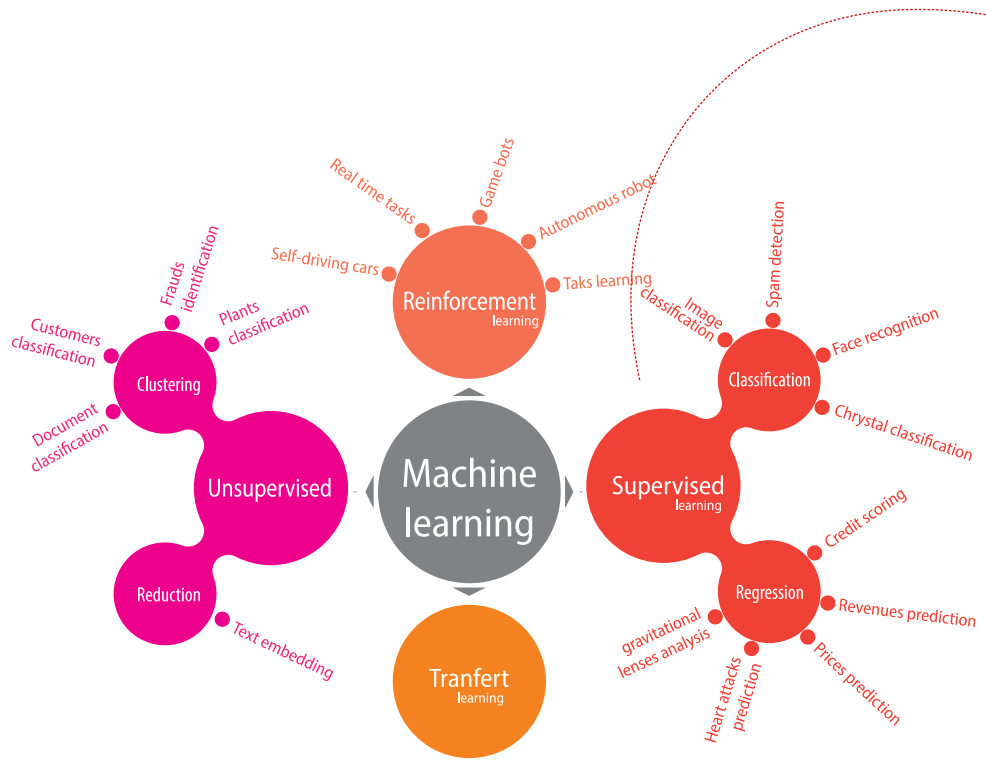


<sup>1</sup> Jim Gray, 2007 [GRAY]

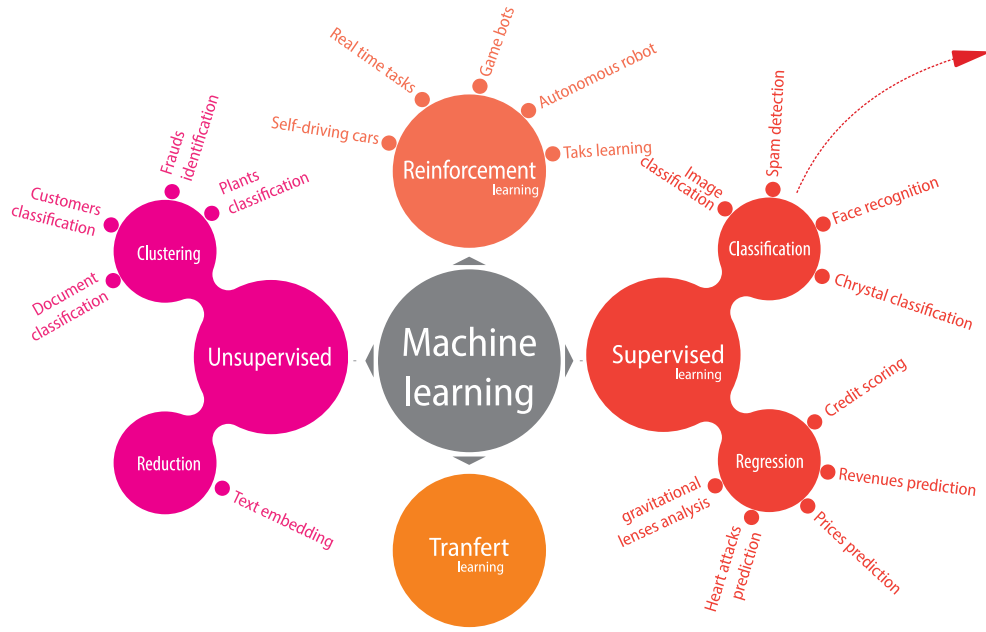




# Supervised learning



Learning from **examples**

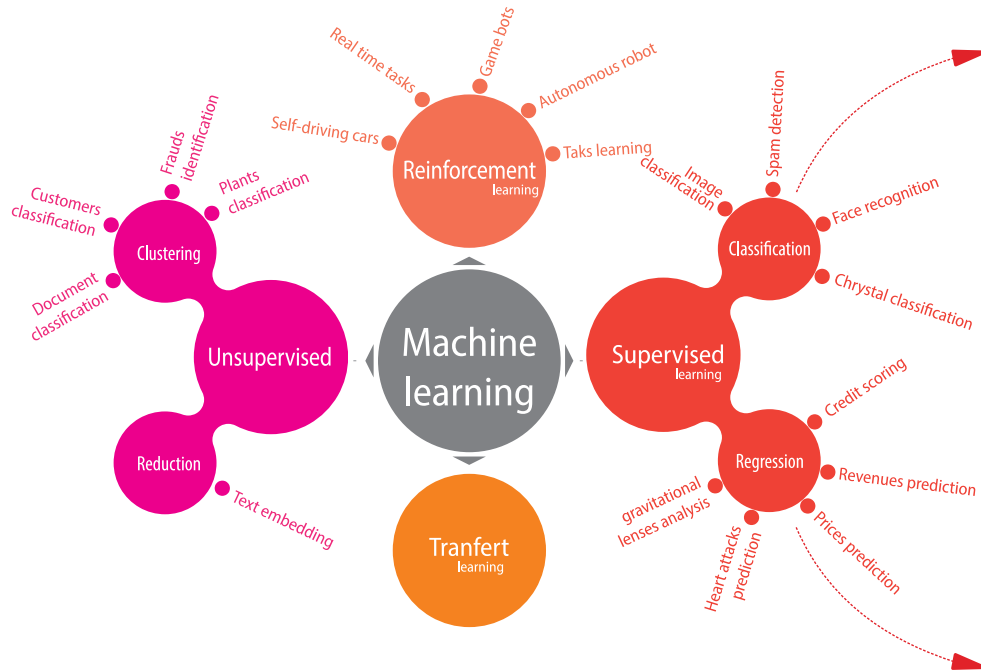


**Classification :**  
Predict qualitative informations

This is a cat

This is a rabbit

Tell me, what is it ?



## Classification :

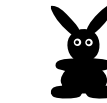
Predict qualitative informations



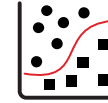
This is a cat



This is a rabbit



Tell me,  
what is it ?



## Régression :

Predict quantitative informations



150 K€



400 K€



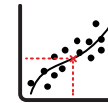
120 K€



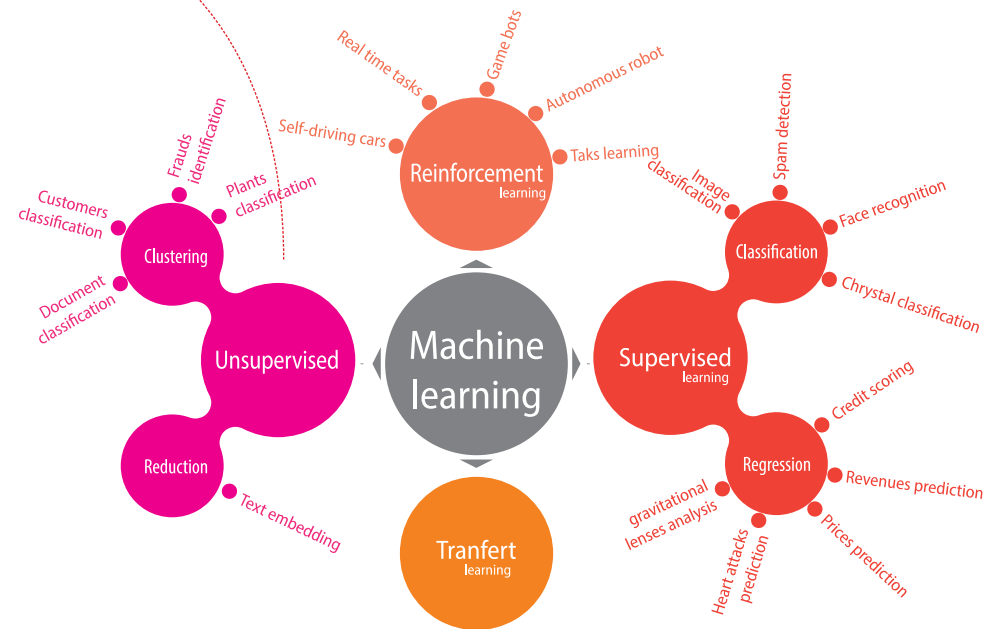
100 K€



Tell me,  
what's  
the  
price ?

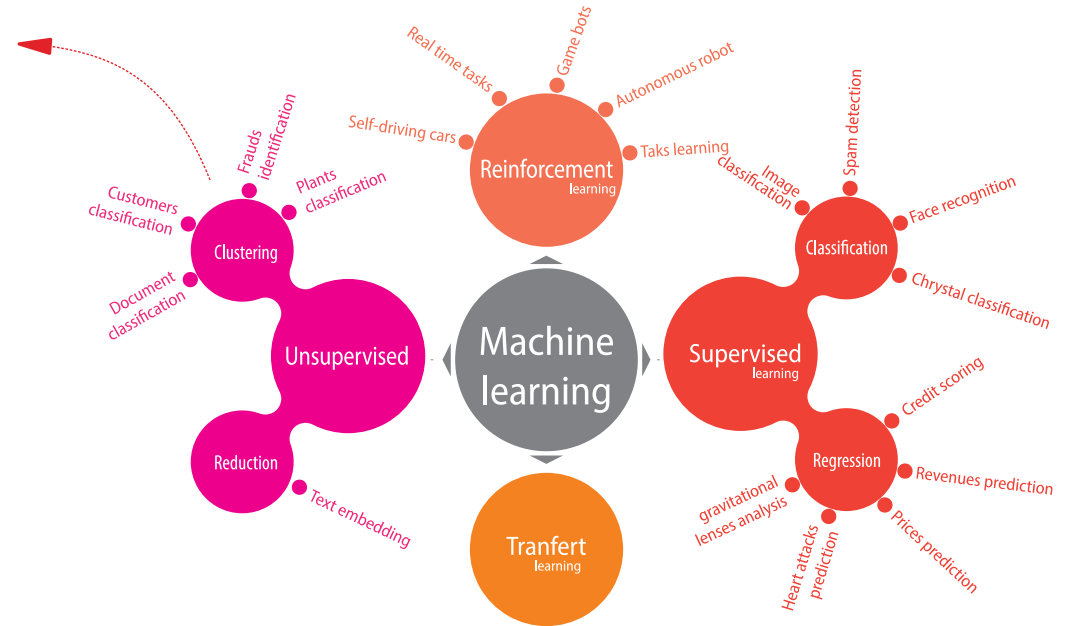
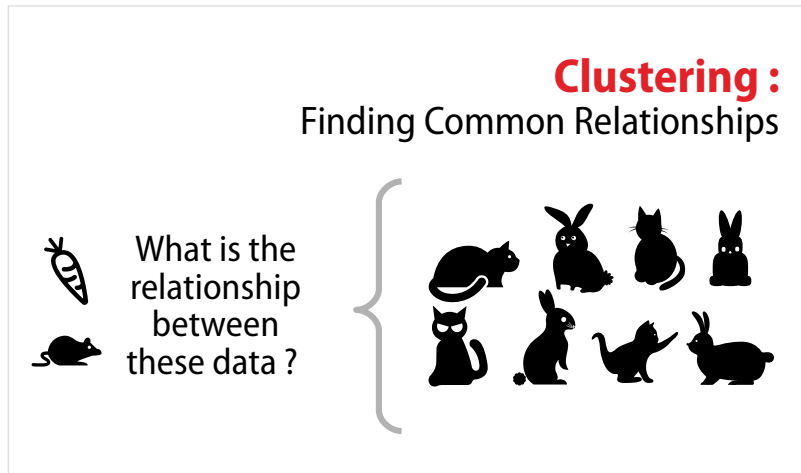


## Learning from data alone



**Clustering:**  
Finding Common Relationships

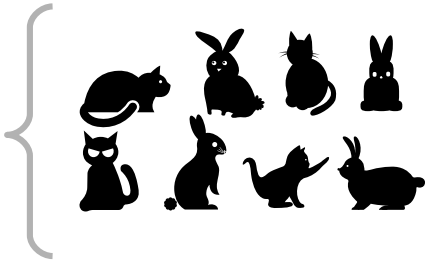
What is the relationship between these data?



**Clustering:**  
Finding Common Relationships



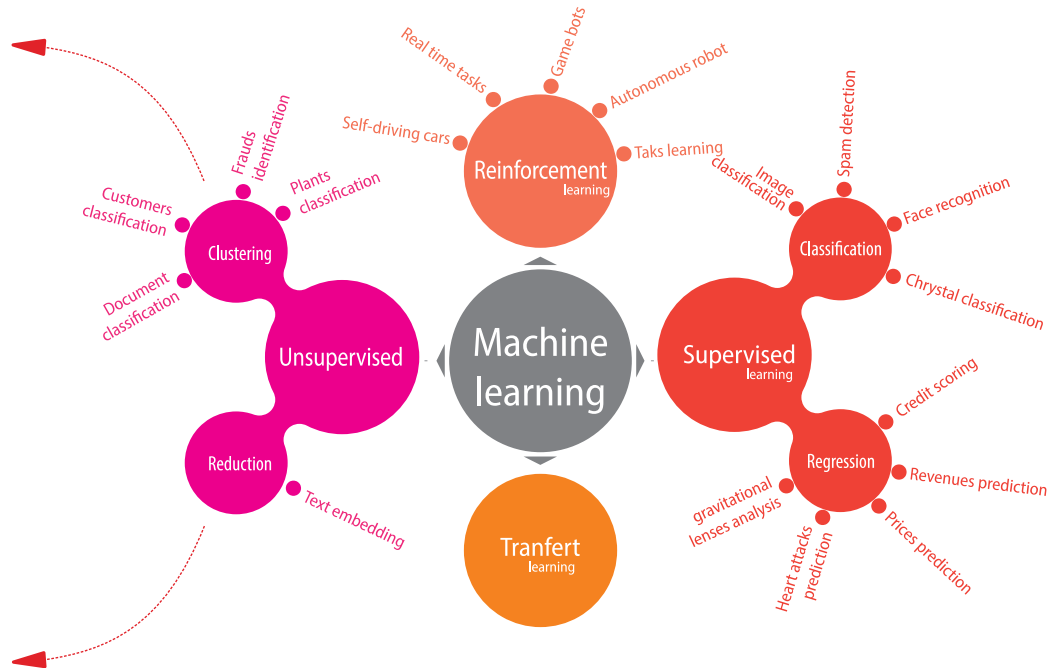
What is the relationship between these data?



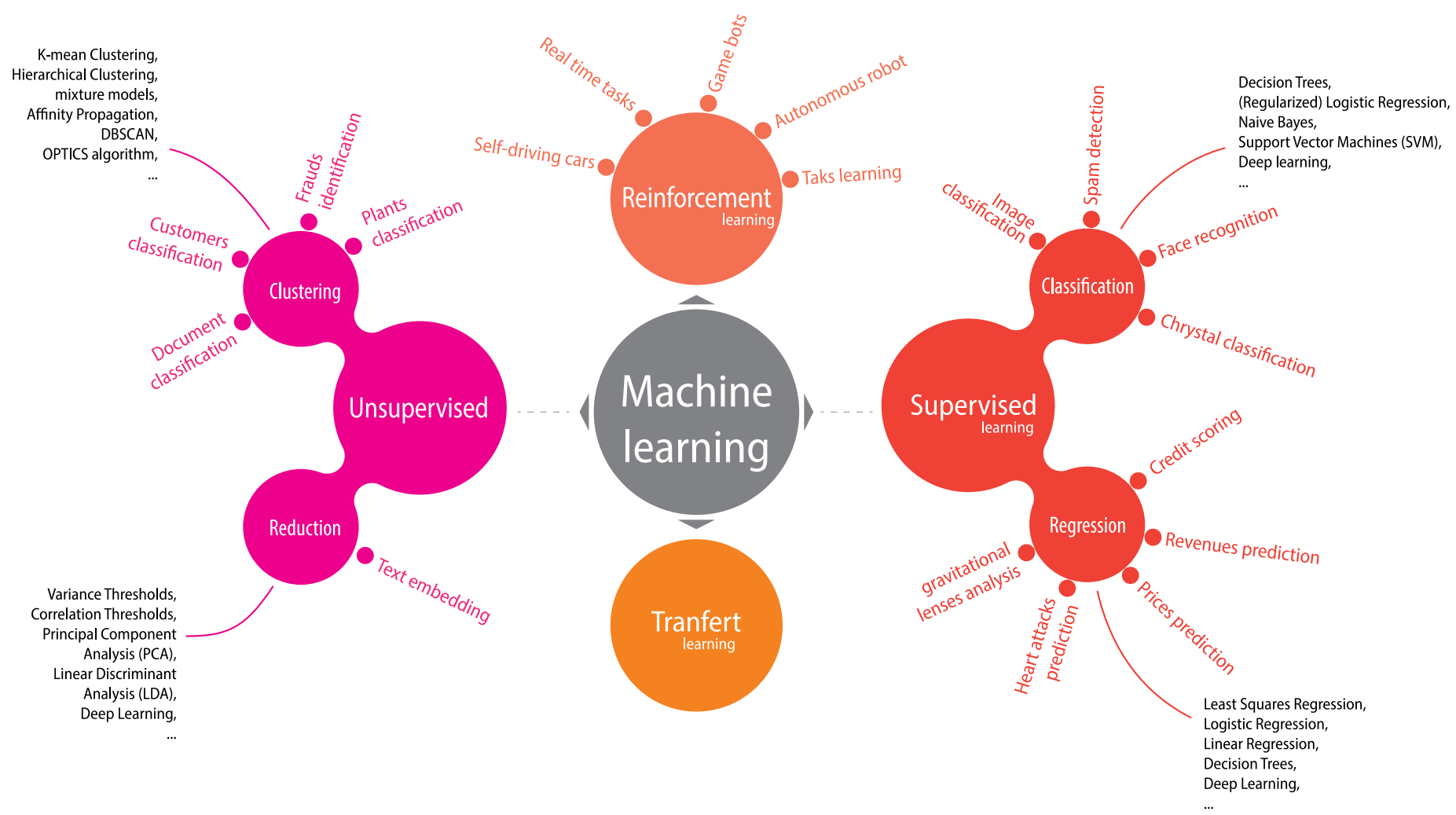
**Reduction:**  
Reduce the number of dimensions

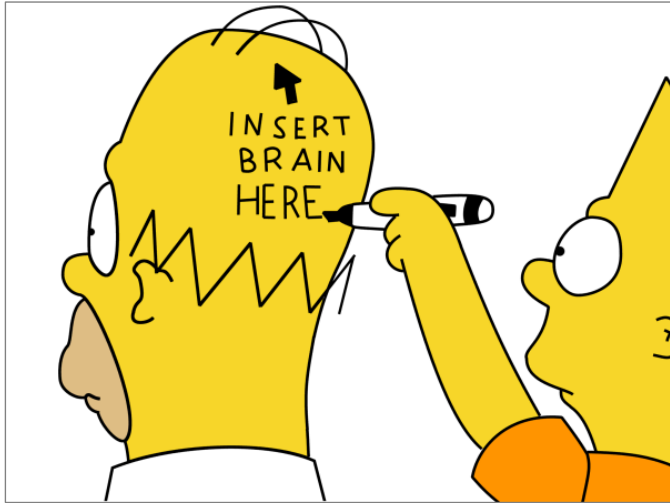


Simplify while keeping meaning



# [ \*-learning ]





Fine, but  
◀ Deep Learning  
What's that?



- 1 From the linear regression to the first neuron
- 2 Neurons in controversy
- 3 Neurons at work !

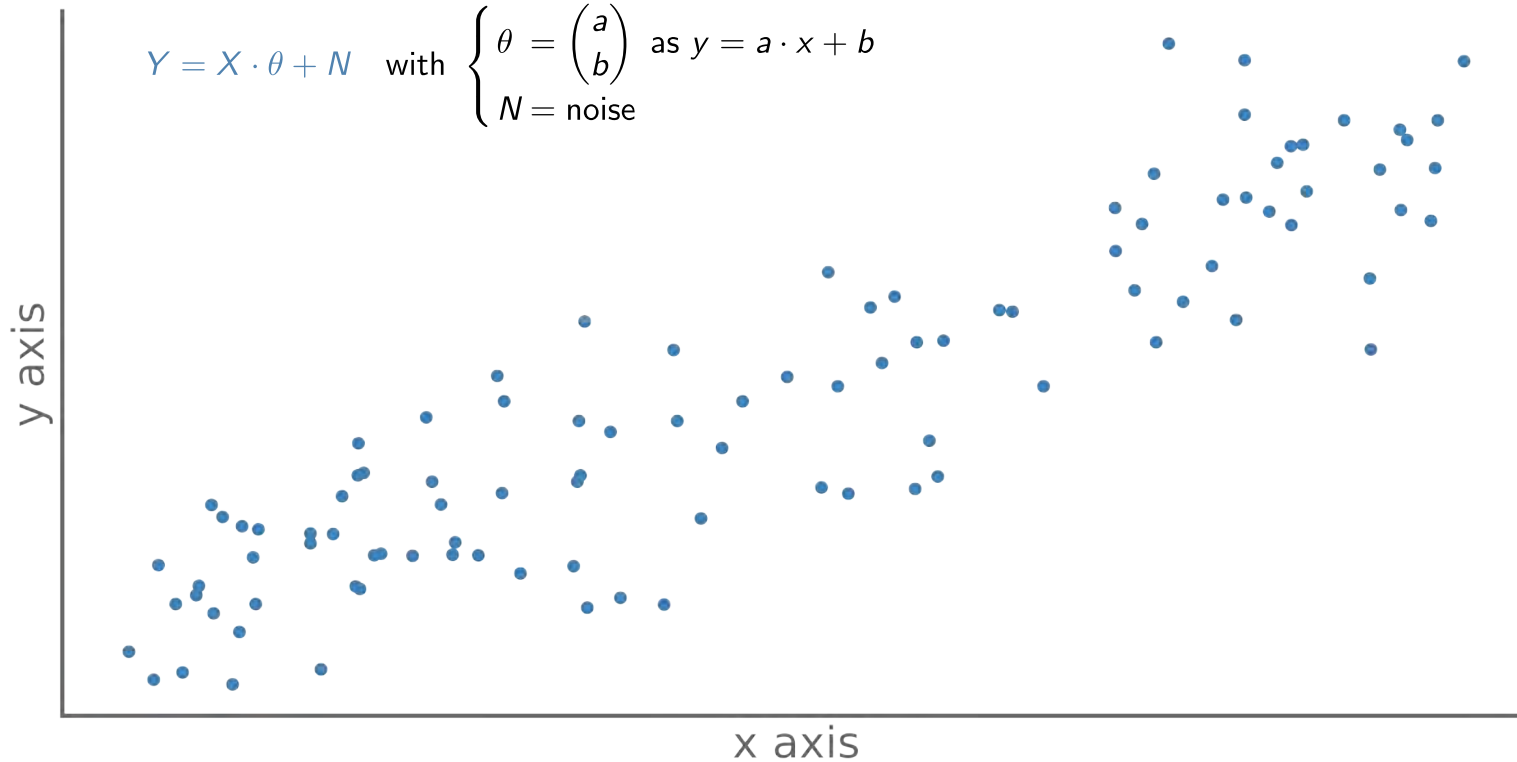


From the linear regression  
to the first neuron

# Linear regression

We have a phenomenon, for which we have observations

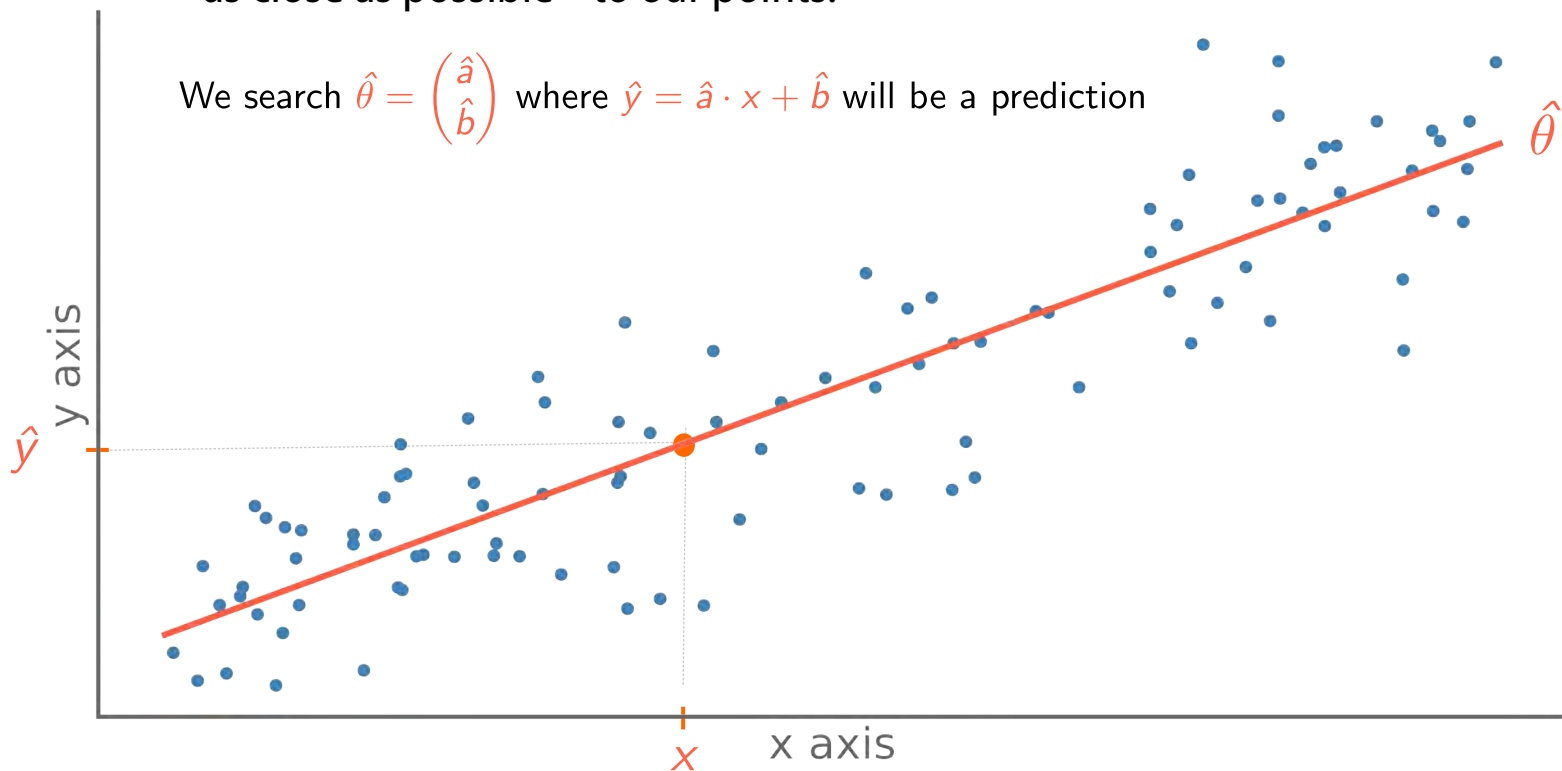
$$Y = X \cdot \theta + N \quad \text{with} \quad \begin{cases} \theta = \begin{pmatrix} a \\ b \end{pmatrix} \text{ as } y = a \cdot x + b \\ N = \text{noise} \end{cases}$$



# Linear regression

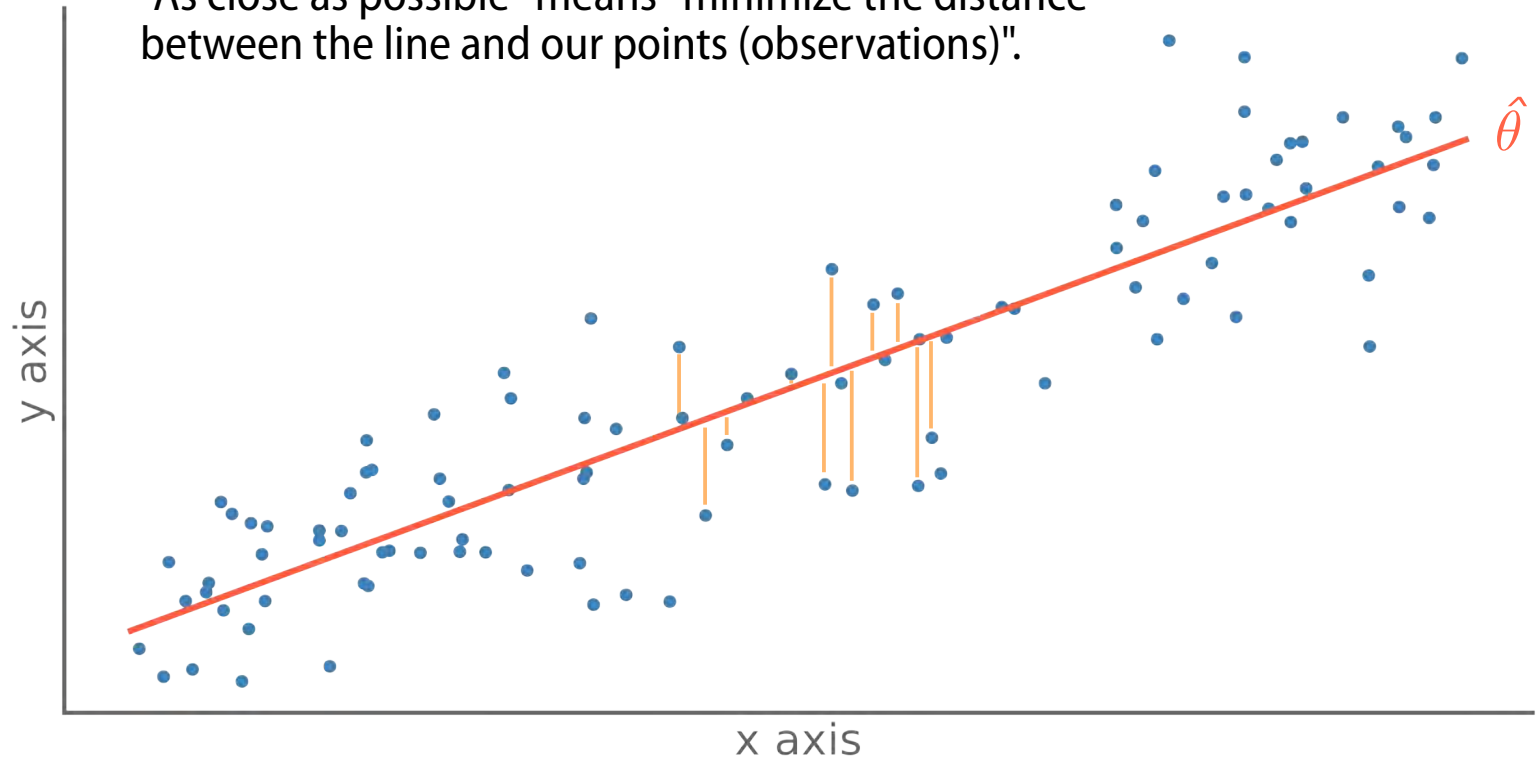
We are looking for a straight line that passes « as close as possible » to our points.

We search  $\hat{\theta} = \begin{pmatrix} \hat{a} \\ \hat{b} \end{pmatrix}$  where  $\hat{y} = \hat{a} \cdot x + \hat{b}$  will be a prediction



# Linear regression

"As close as possible" means "minimize the distance between the line and our points (observations)".

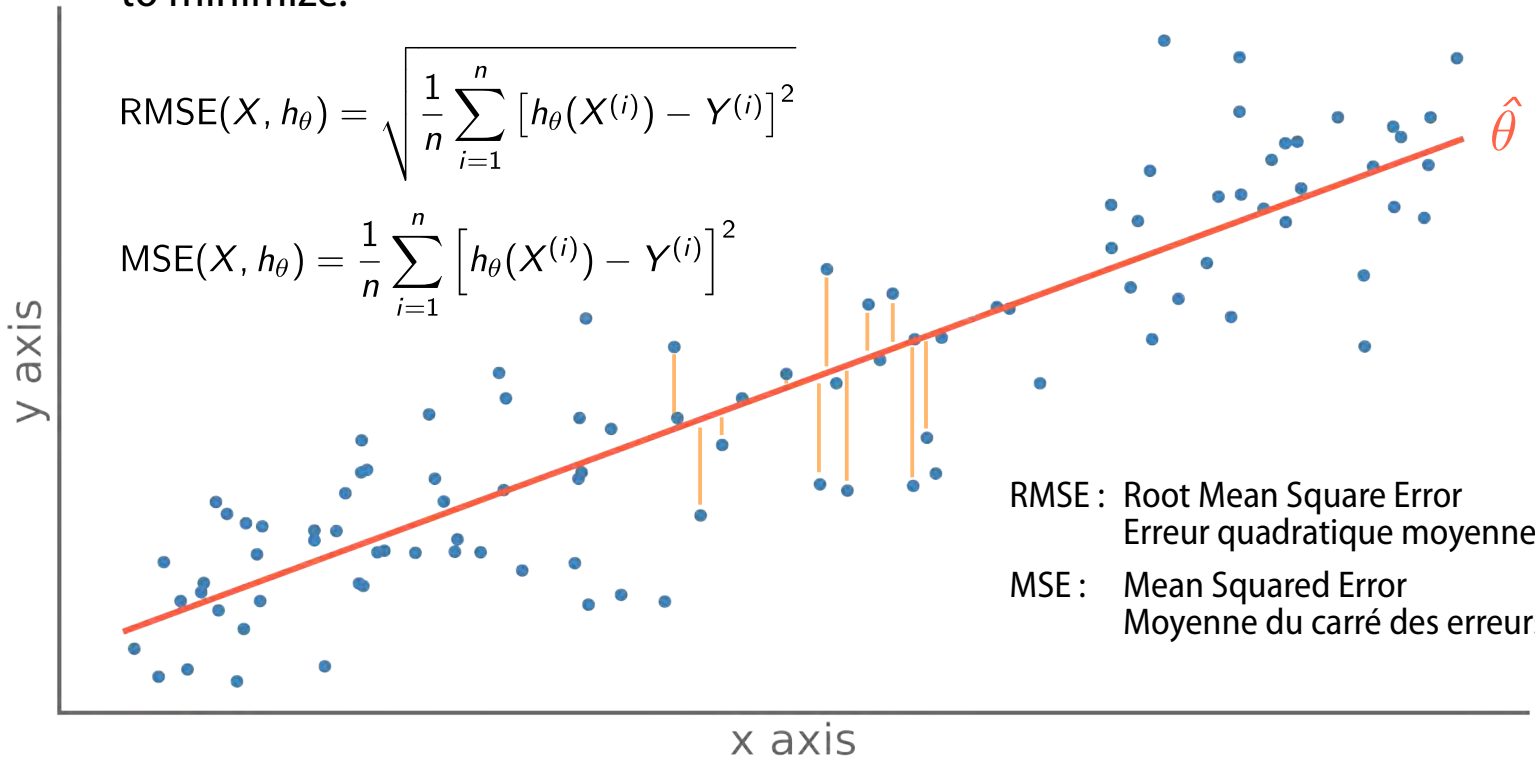


# Linear regression

For this, we will use an «loss function », which we will try to minimize.

$$\text{RMSE}(X, h_{\theta}) = \sqrt{\frac{1}{n} \sum_{i=1}^n [h_{\theta}(X^{(i)}) - Y^{(i)}]^2}$$

$$\text{MSE}(X, h_{\theta}) = \frac{1}{n} \sum_{i=1}^n [h_{\theta}(X^{(i)}) - Y^{(i)}]^2$$



RMSE : Root Mean Square Error  
Erreur quadratique moyenne

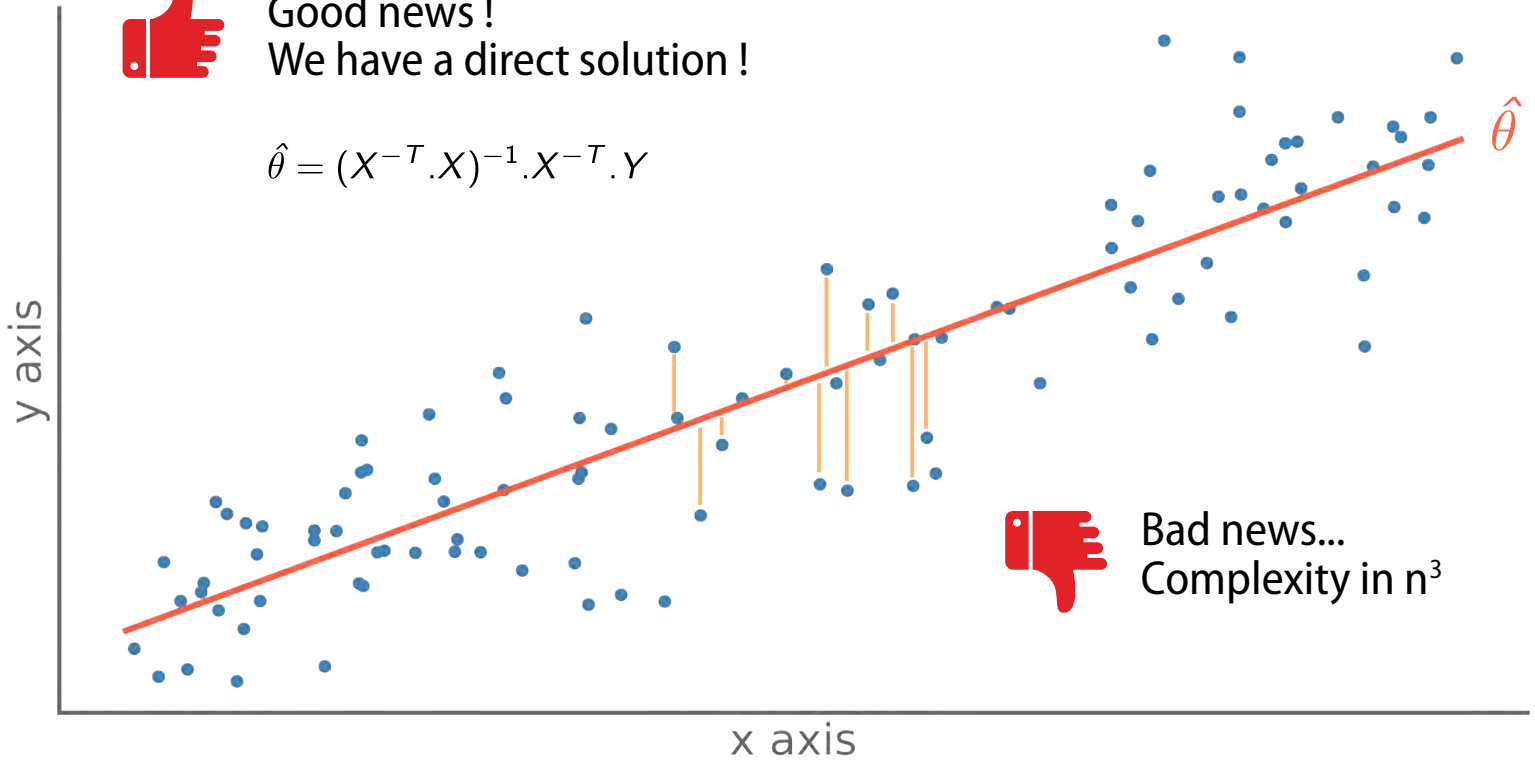
MSE : Mean Squared Error  
Moyenne du carré des erreurs

# Linear regression



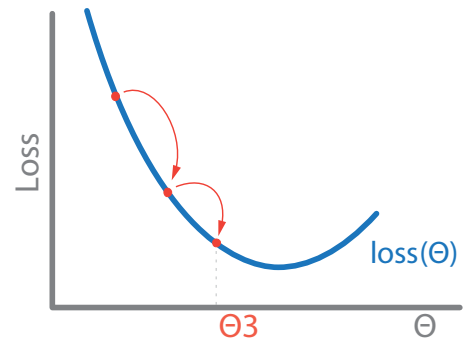
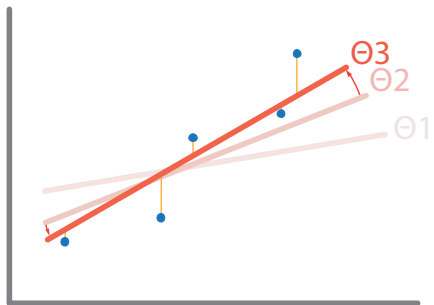
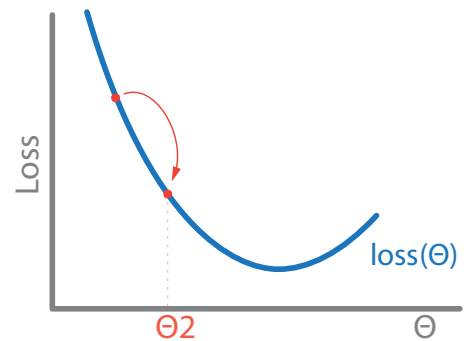
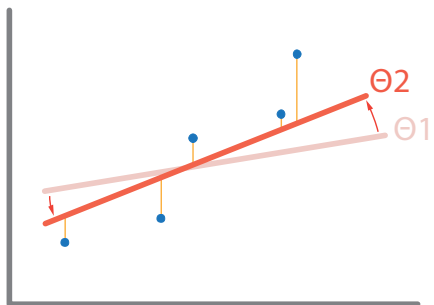
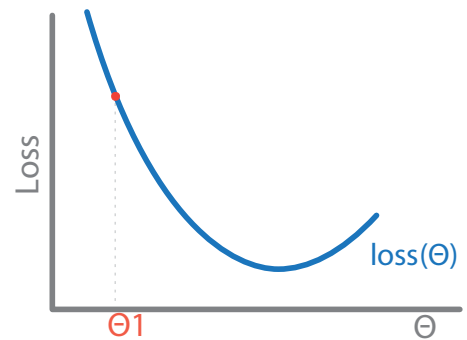
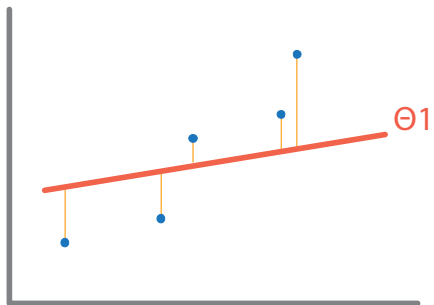
Good news!  
We have a direct solution!

$$\hat{\theta} = (X^{-T} \cdot X)^{-1} \cdot X^{-T} \cdot Y$$



Bad news...  
Complexity in  $n^3$

# Gradient descent



We will iteratively look for the best position of our line, by varying its parameters ( $\Theta$ ).



But how can we efficiently vary our parameters ( $\Theta$ )?

Note:

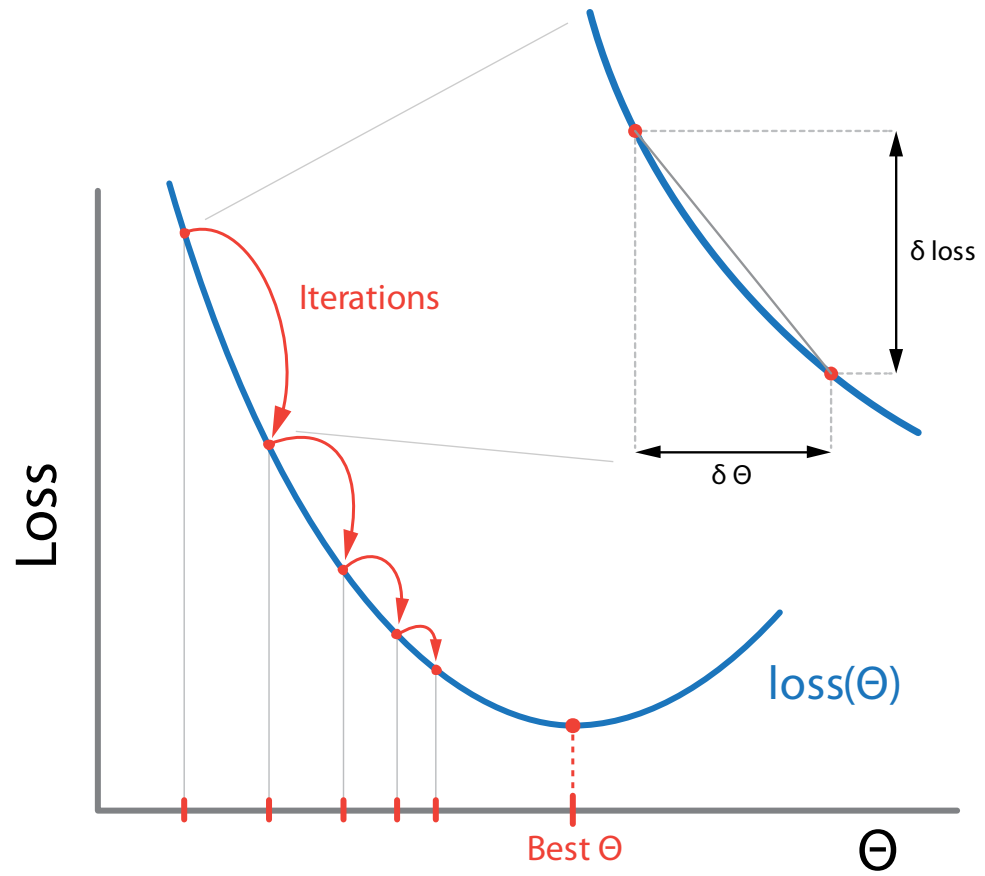
Loss functions could be :

$$\text{RMSE}(X, h_\theta) = \sqrt{\frac{1}{n} \sum_{i=1}^n [h_\theta(X^{(i)}) - Y^{(i)}]^2}$$

$$\text{MSE}(X, h_\theta) = \frac{1}{n} \sum_{i=1}^n [h_\theta(X^{(i)}) - Y^{(i)}]^2$$



# Gradient descent



By changing  $\Theta$  from  $\delta\Theta$   
We improve  $\text{loss}(\Theta)$  of  $\delta\text{loss}$

The gradient is the slope we will follow to minimize our loss function.

$$\text{gradient} = \frac{\delta\text{loss}}{\delta\theta}$$

One iterative solution is :  $\theta \leftarrow \theta - \eta \cdot \frac{\delta\text{loss}}{\delta\theta}$

where  $\eta$  is the learning rate

This process is called **gradient descent** and the function used to optimize the descent, **optimization** function

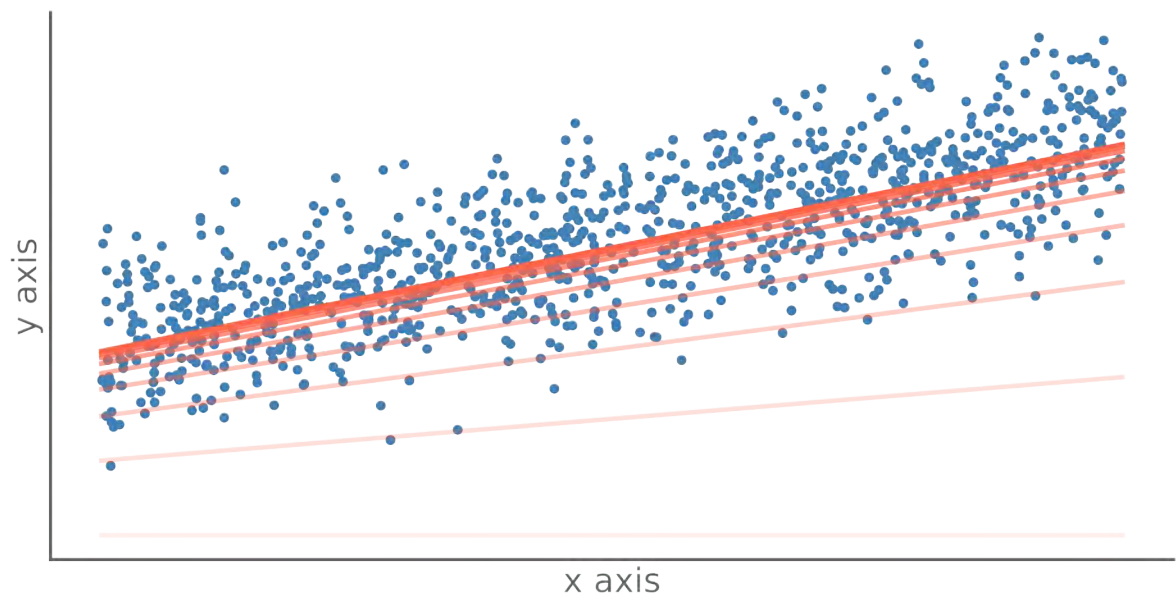
# Gradient descent

$$MSE(X, h_{\theta}) = \frac{1}{n} \sum_{i=1}^n [h_{\theta}(X^{(i)}) - Y^{(i)}]^2$$

$$\nabla_{\theta} MSE(\Theta) = \begin{bmatrix} \frac{\partial}{\partial \theta_0} MSE(\Theta) \\ \frac{\partial}{\partial \theta_1} MSE(\Theta) \\ \vdots \\ \frac{\partial}{\partial \theta_m} MSE(\Theta) \end{bmatrix} = \frac{2}{n} X^T \cdot (X \cdot \Theta - Y)$$

Iterative solution is :  $\Theta \leftarrow \Theta - \eta \cdot \nabla_{\theta} MSE(\Theta)$   
where  $\eta$  is the learning rate

n : number of observations  
m : number of characteristics

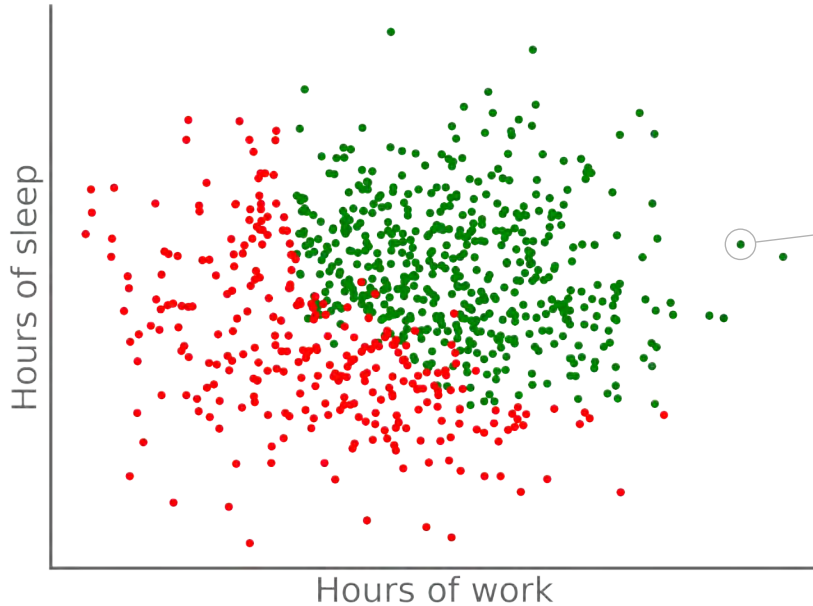


#i	Loss	Gradient		Theta	
0	+12.481	-6.777	-1.732	-3.388	+0.000
20	+4.653	-4.066	-1.039	-2.033	+0.346
40	+1.835	-2.440	-0.624	-1.220	+0.554
60	+0.821	-1.464	-0.374	-0.732	+0.679
80	+0.455	-0.878	-0.224	-0.439	+0.754
100	+0.324	-0.527	-0.135	-0.263	+0.799
120	+0.277	-0.316	-0.081	-0.158	+0.826
140	+0.260	-0.190	-0.048	-0.095	+0.842
160	+0.253	-0.114	-0.029	-0.057	+0.851
180	+0.251	-0.068	-0.017	-0.034	+0.857
200	+0.250	-0.041	-0.010	-0.020	+0.861

# Logistic regression

A logistic regression is intended to provide a probability of belonging to a class.

**Dataset :** X Observations  
y Classe

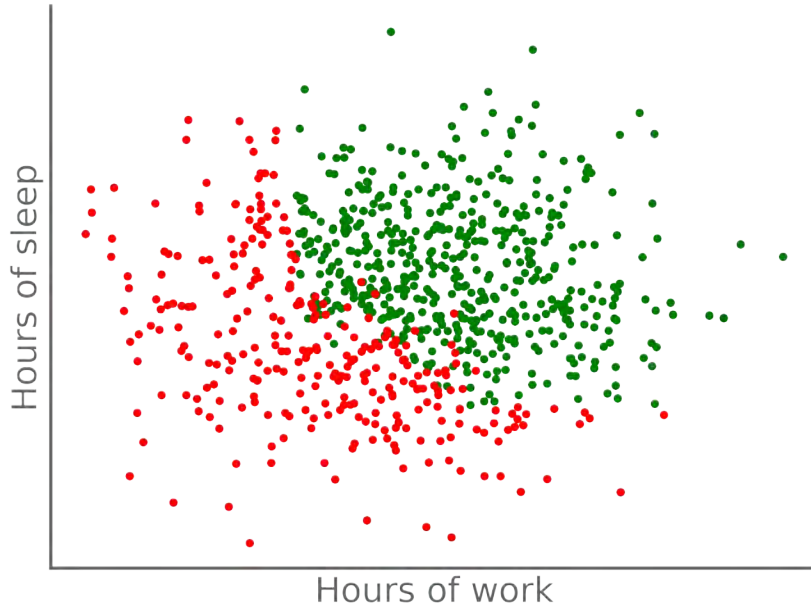


$$(X_i, y_i) \begin{cases} X_i = \begin{pmatrix} x_{i1} = \text{Hours of work} \\ x_{i2} = \text{Hours of sleep} \end{pmatrix} \\ y_i = \begin{cases} 1 & \text{belong to the class} \\ 0 & \text{don't belong} \end{cases} \end{cases}$$

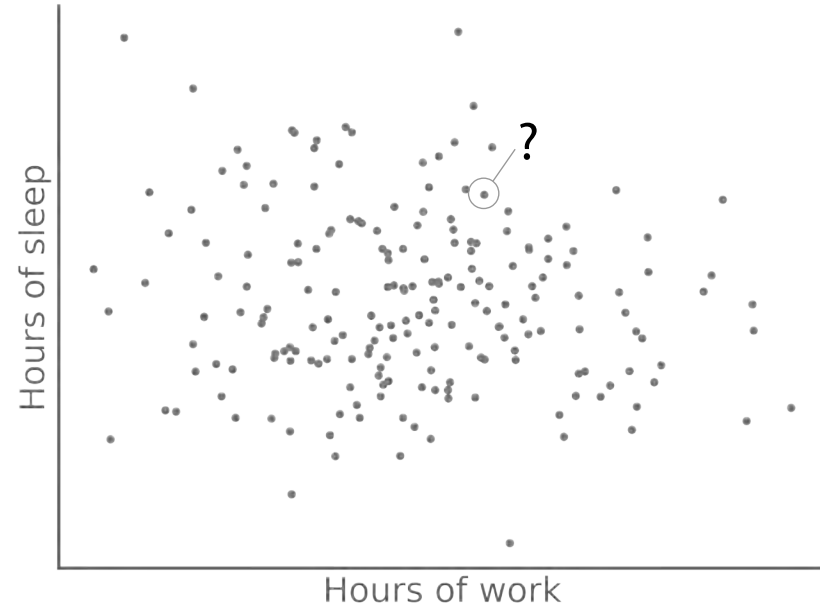
# Logistic regression

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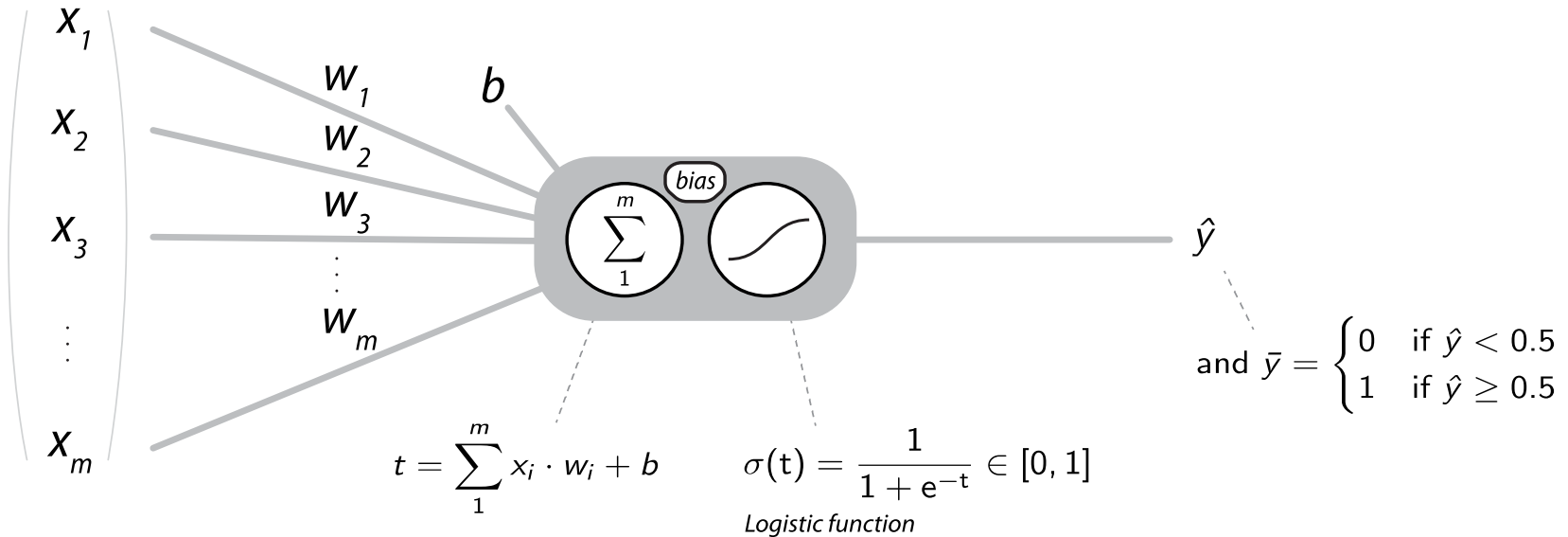


**Objective :** Predict the class  
x given, we want to predict y  
 $\mathbf{y}_{\text{pred}} = \mathbf{f}(\mathbf{x})$   
where f is a linear function



# Logistic regression

$$\hat{y} = \sigma(\Theta^T \cdot X + b)$$



**Input**

$X$

**Bias / Weight**

$\Theta$

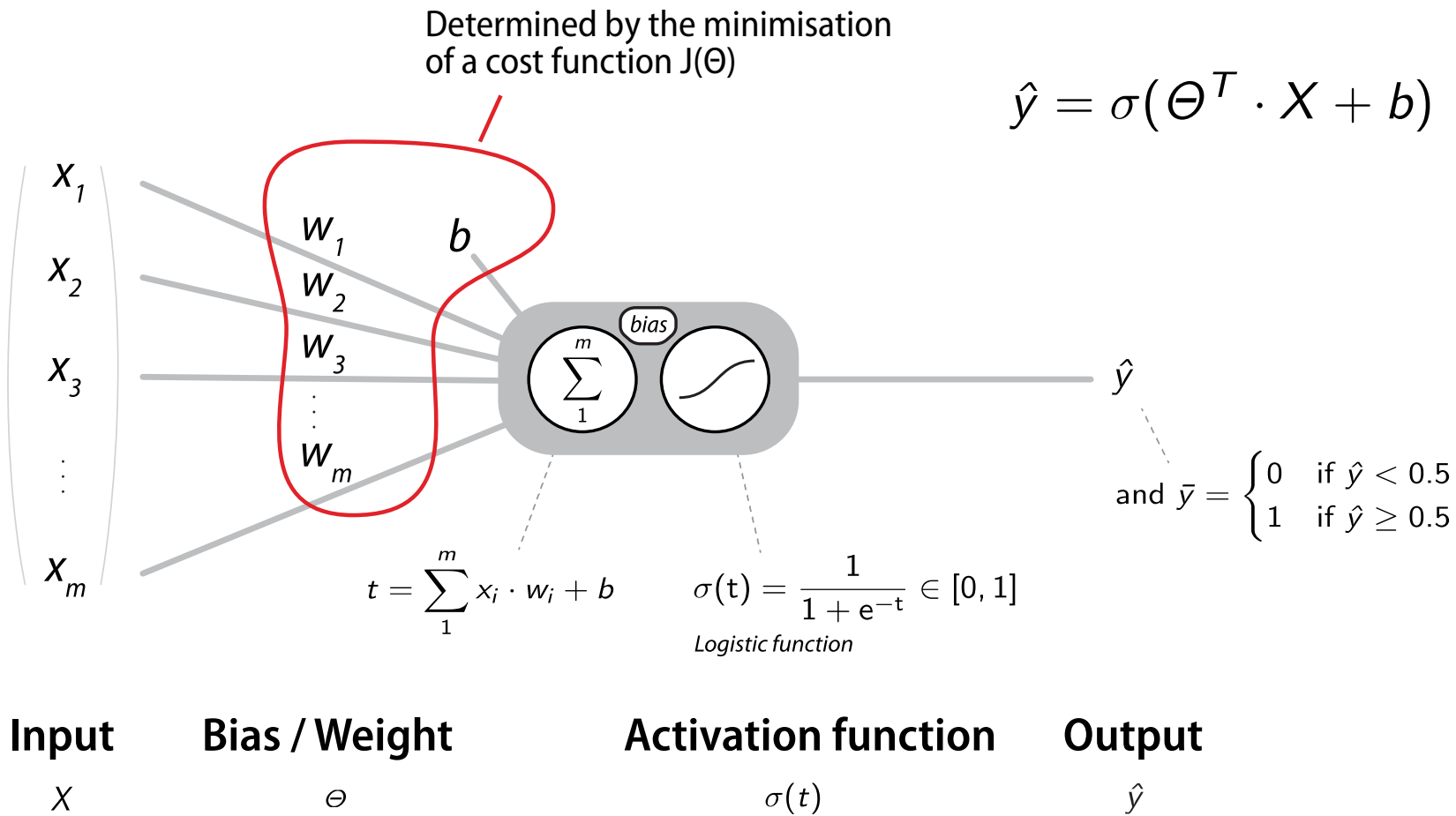
**Activation function**

$\sigma(t)$

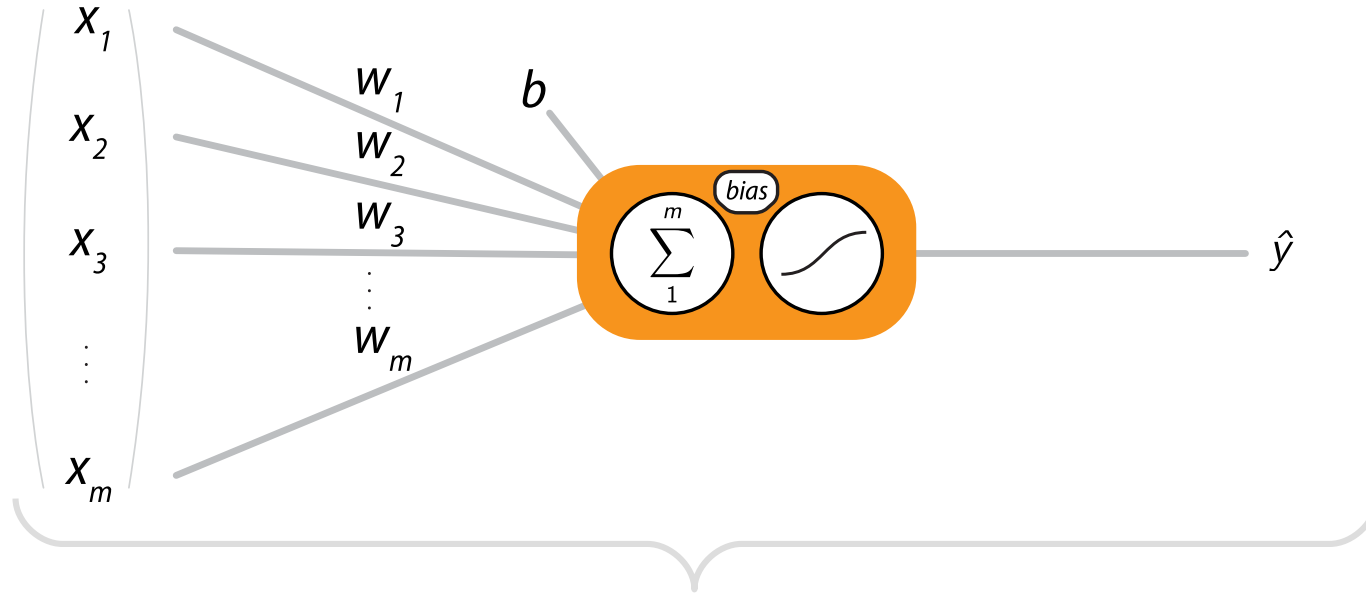
**Output**

$\hat{y}$

# Logistic regression

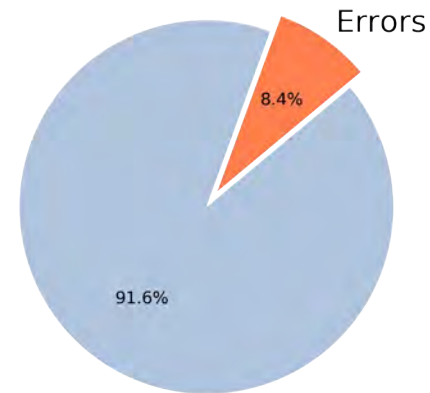
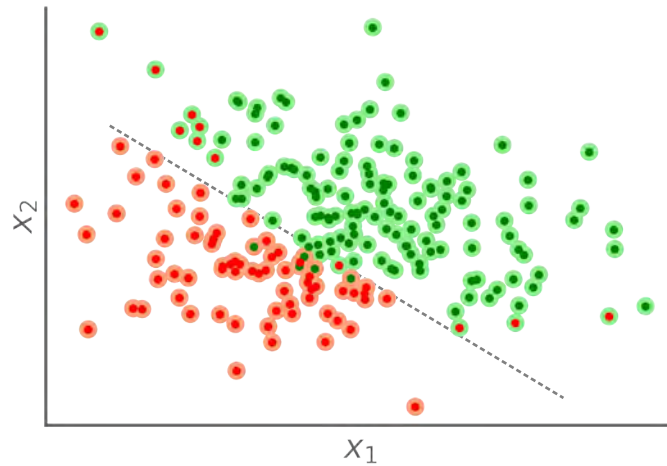
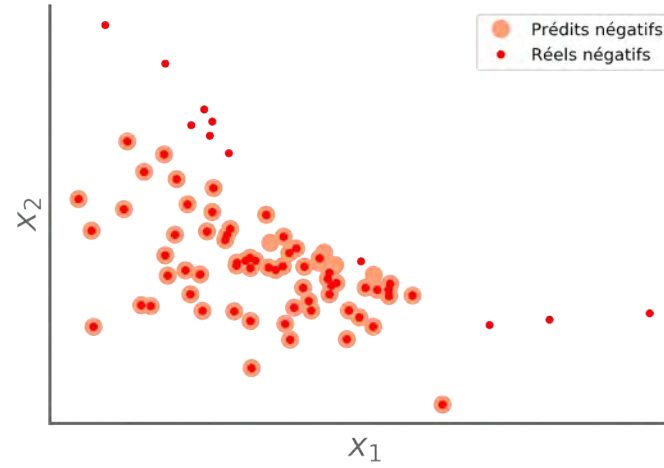
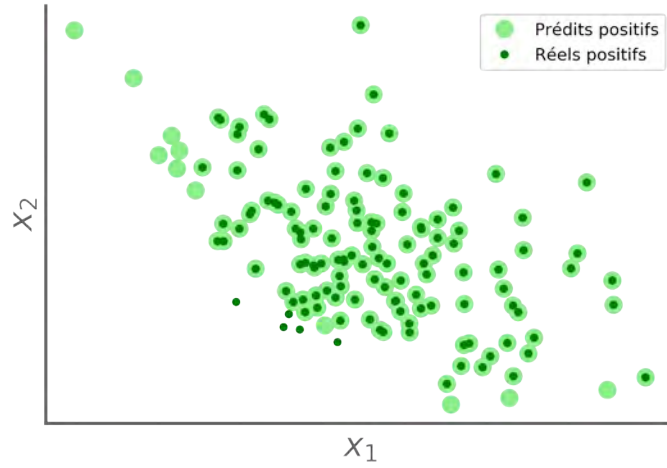


$$\hat{y} = \sigma(\Theta^T \cdot X + b)$$



That's an « **artificial neuron** » !  
So, we have a neural network of... 1 neuron !

# Logistic regression





## 2 Neurons in controversy<sup>1</sup>

Dominique Cardon, Jean-Philippe Cointet, Antoine Mazieres. La revanche des neurones : L'invention des machines inductives et la controverse de l'intelligence artificielle. Réseaux, La Découverte, 2018, 5 (211), <10.3917/res.211.0173>. <hal-01925644>

[ intelligence ]



# [ intelligence ]

« Ability to perceive or infer information, and to retain it as knowledge to be applied towards adaptive behaviors within an environment or context »\*

« Capacité de percevoir ou d'inférer l'information, et de la conserver comme une connaissance à appliquer à des comportements adaptatifs dans un environnement ou un contexte donné »



# [ intelligence ]

« Set of mental **functions** aimed at **conceptual** and **rational** knowledge »

« Ensemble des **fonctions** mentales ayant pour objet la connaissance **conceptuelle** et **rationnelle** »\*

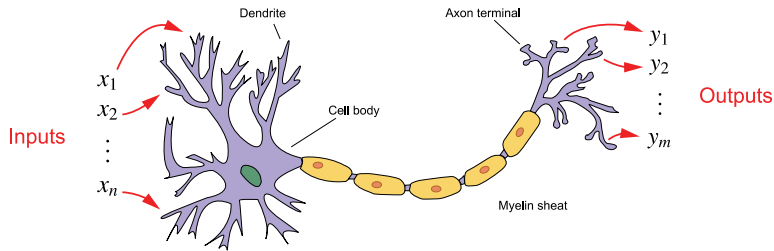
*Modelling the brain :*

Thinking is the result of **elementary** and **massively parallel** functions.

Information is a **signal**

Connectionism

*Modelling the brain  
Modéliser le cerveau*



VS

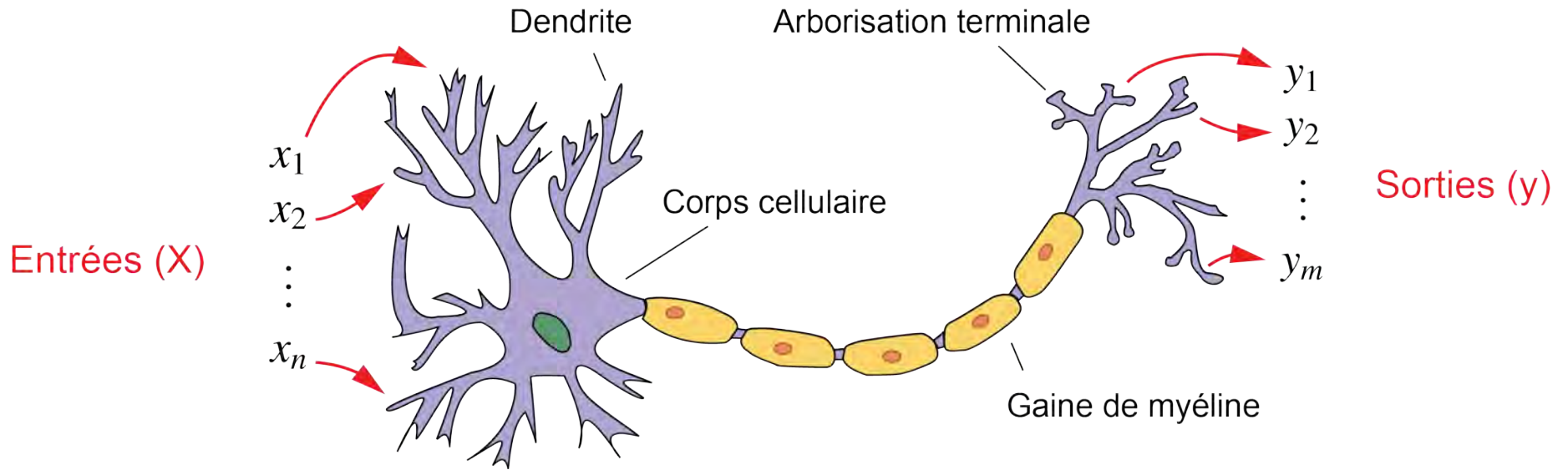
Symbolic

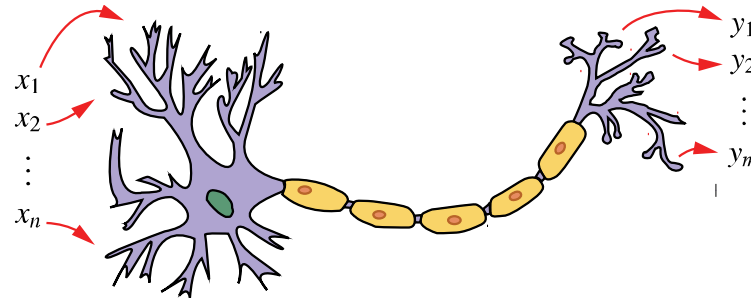
*Making a mind  
Forger une opinion*

Every [man] is [mortal]

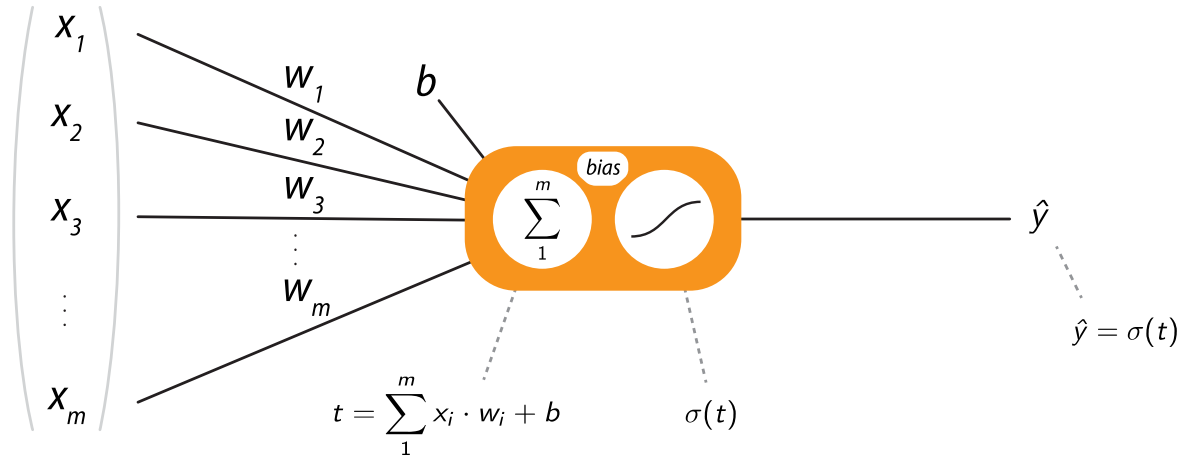
[Socrates] is a [man]

Therefore [Socrates] is [mortal]





$$\hat{y} = \sigma(\Theta^T \cdot X + b)$$



**Input**  
 $X$

**Bias / Weight**  
 $\Theta, b$

**Activation function**  
 $\sigma(t)$

**Output**  
 $\hat{y}$

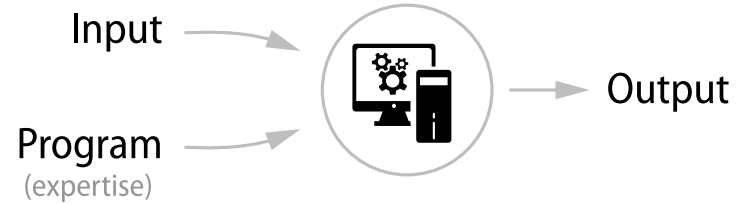
### Inductive approach



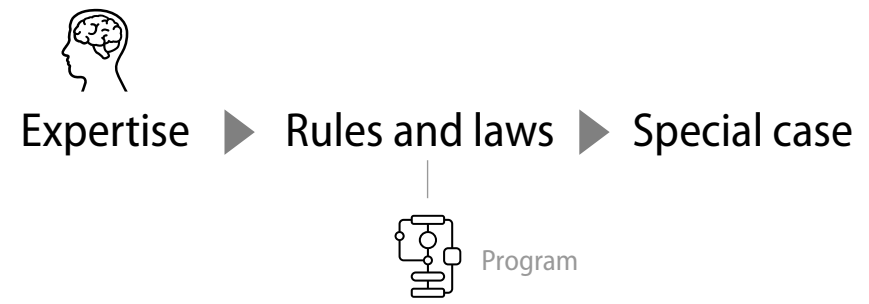
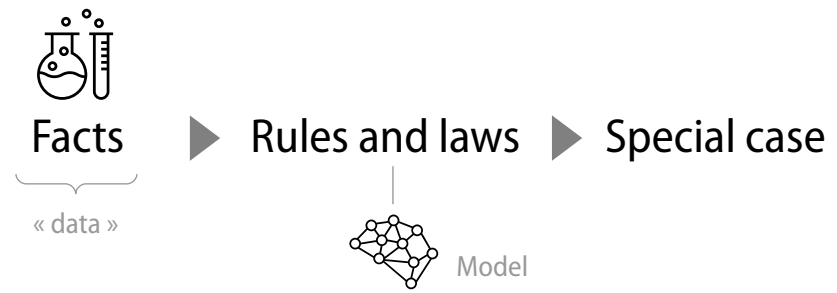
Connectionnism

vs

### Deductive approach



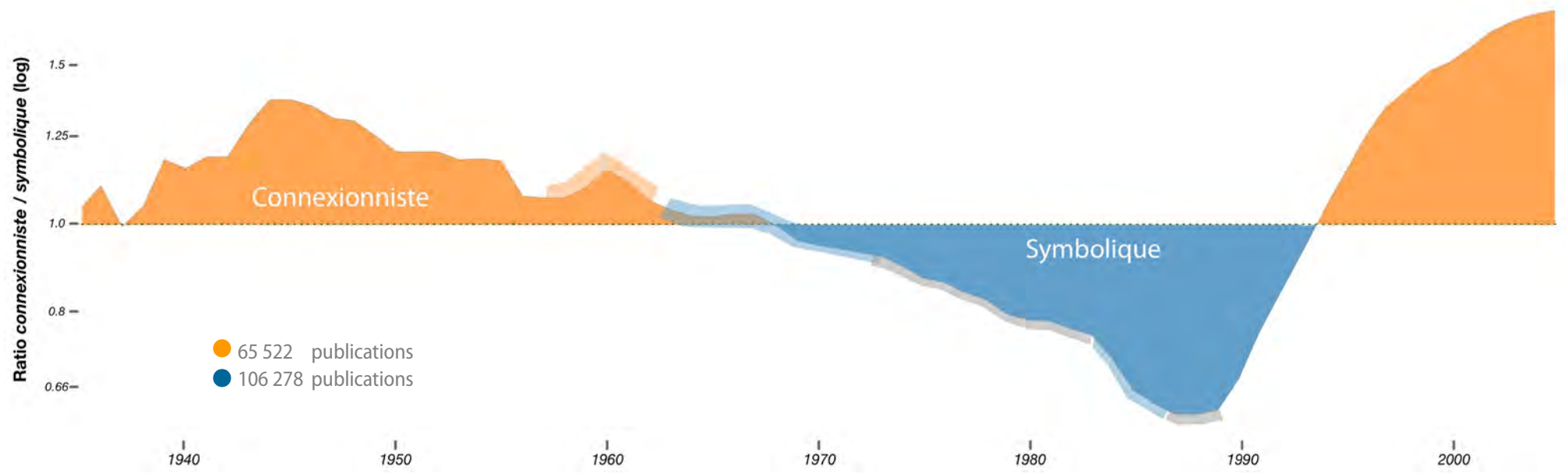
Symbolic





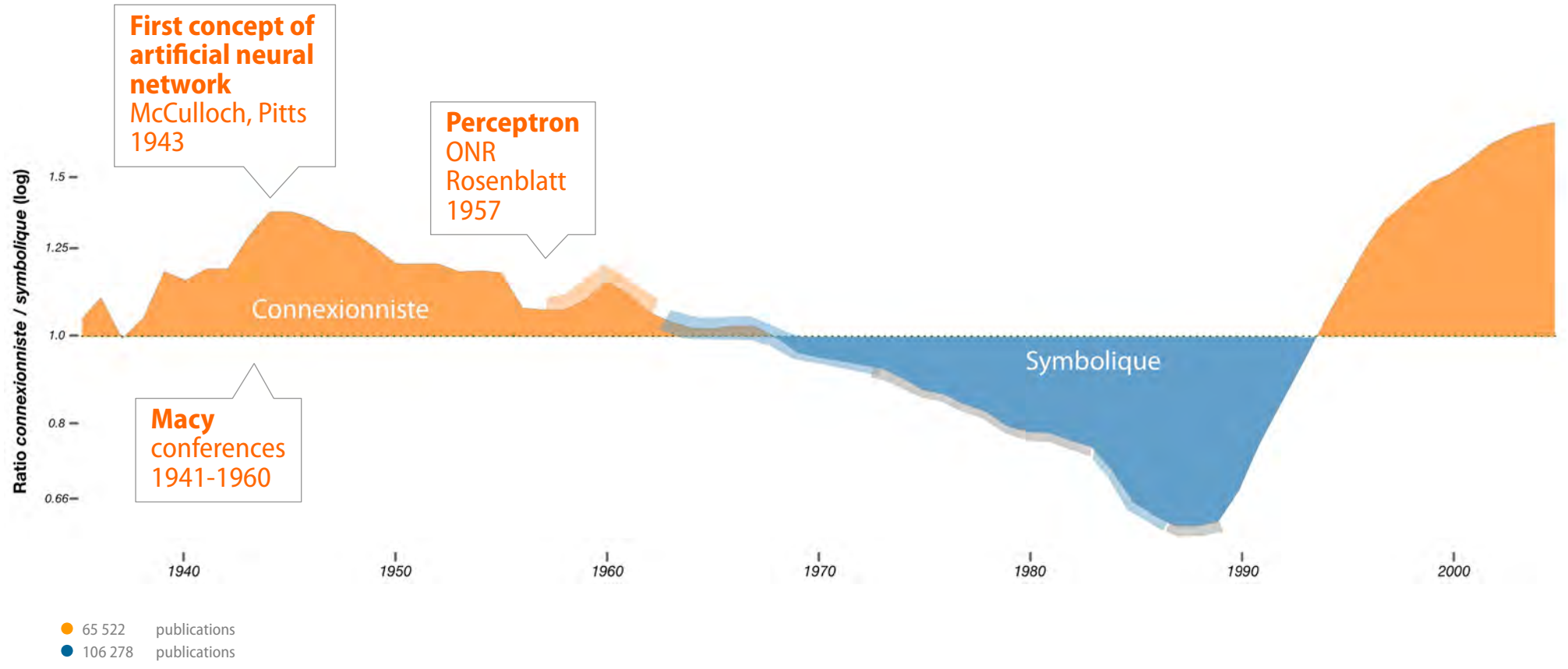
# Evolution of the academic influence of connexionist and symbolic approaches<sup>1</sup>

Ration of publications between connexionists and symbolists



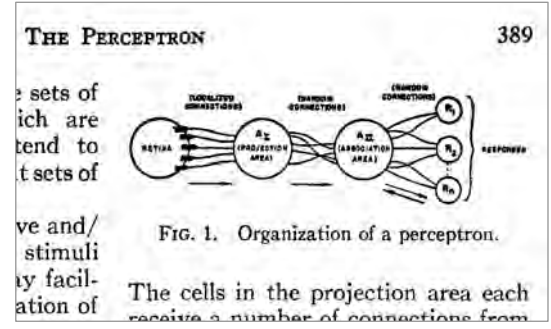
<sup>1</sup> D Cardon, JP Cointet, A Mazieres, 2018 [LRDN]

# Evolution of the academic influence of connexionist and symbolic approaches<sup>1</sup>

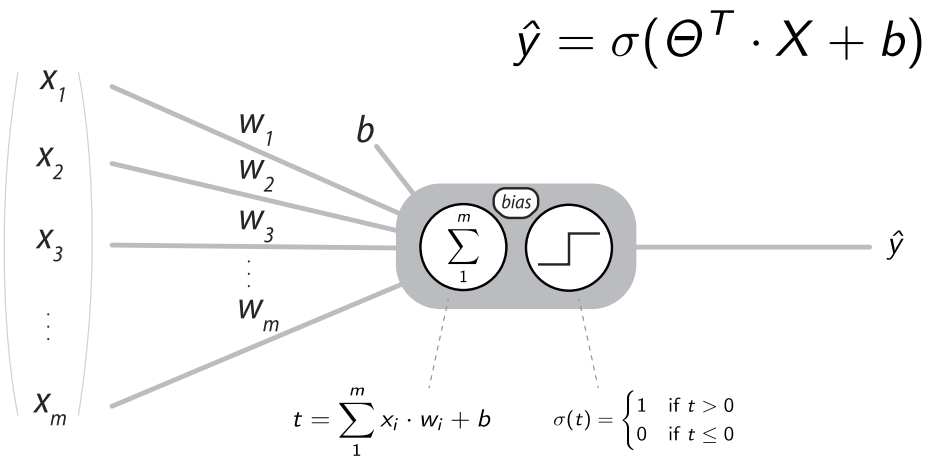


<sup>1</sup> D Cardon, JP Cointet, A Mazieres, 2018 [LRDN]

# Perceptron



Perceptron  
Frank Rosenblatt  
1958

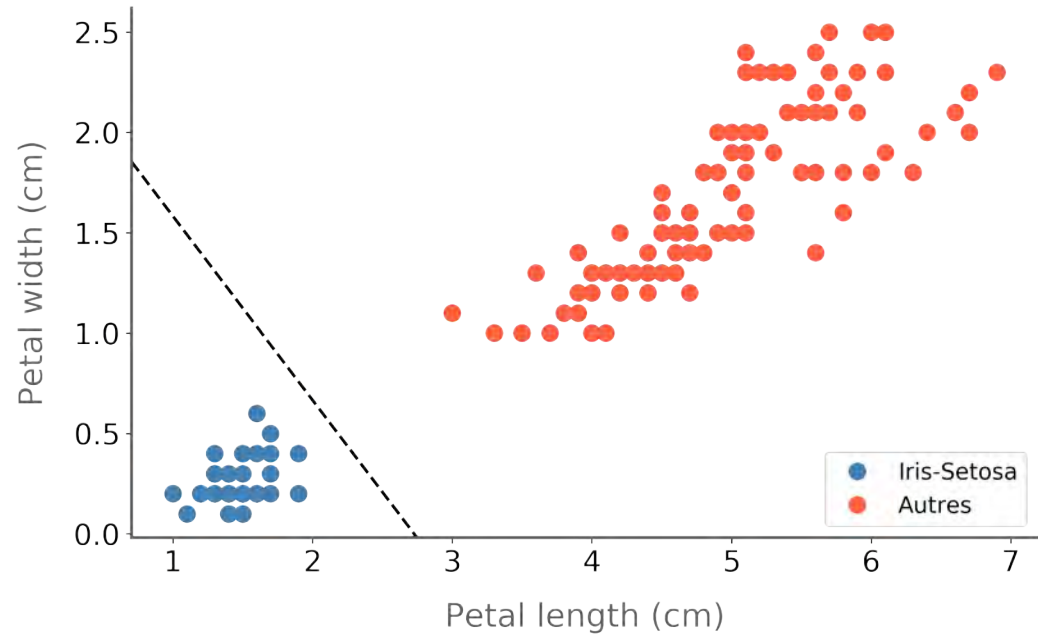


Linear and binary classifier



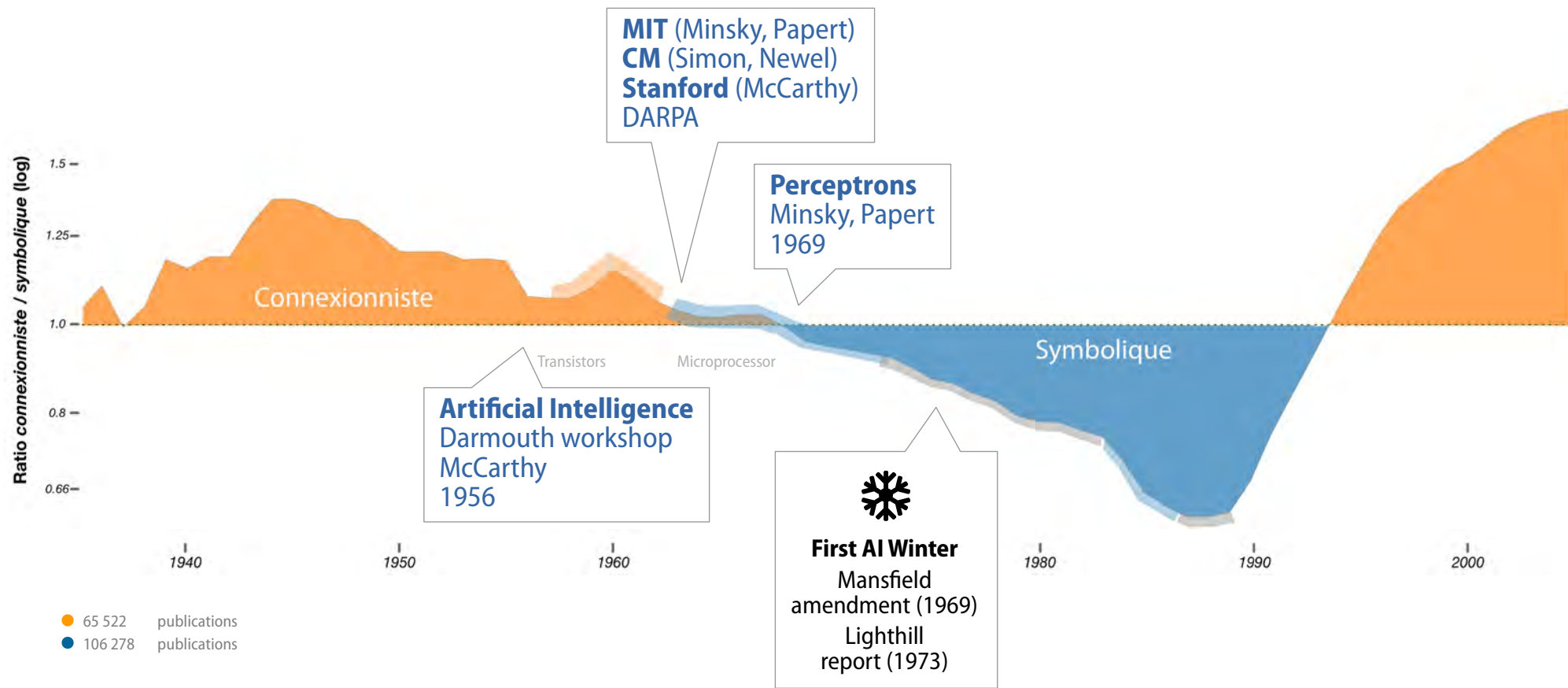
## Iris plants dataset

Dataset from : Fisher, R.A. "The use of multiple measurements in taxonomic problems" Annual Eugenics, 7, Part II, 179-188 (1936)



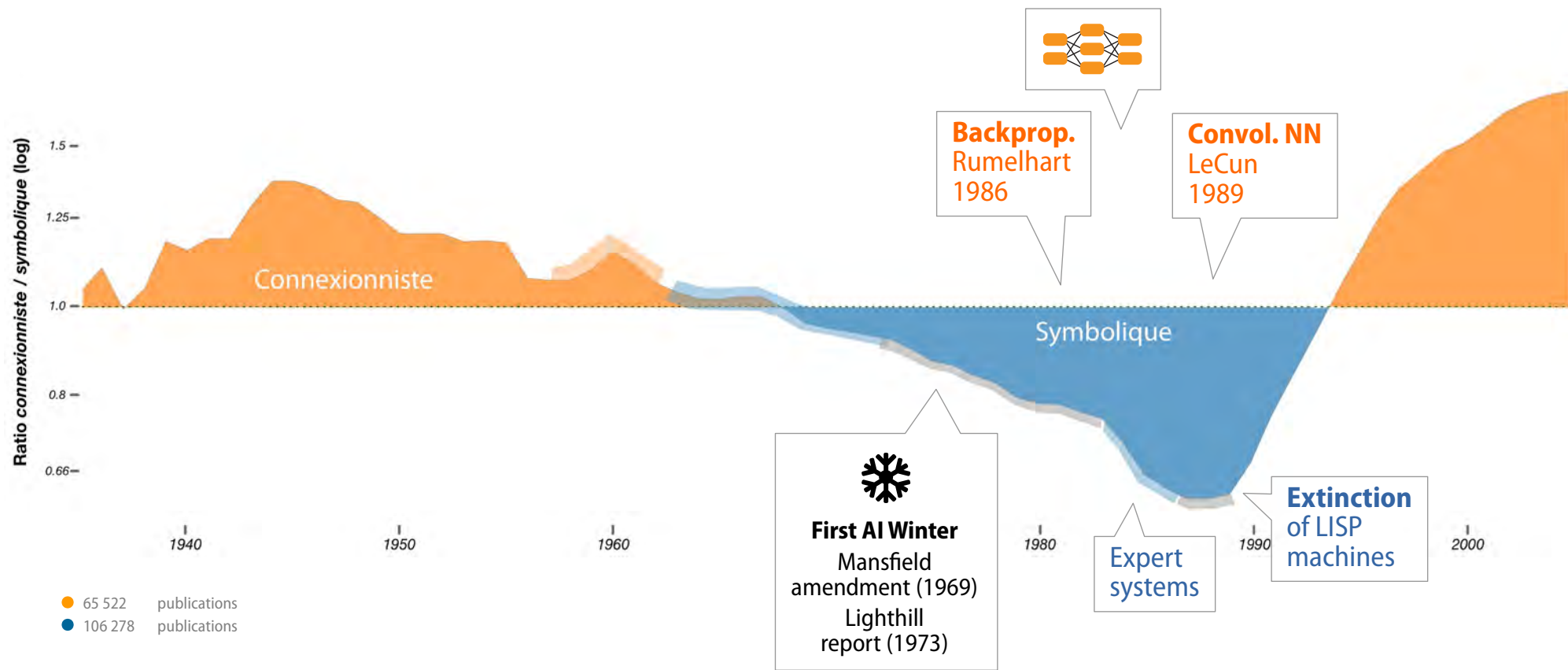
Length	Width	Iris Setosa (0/1)
$x_1$	$x_2$	$y$
1.4	1.4	1
1.6	1.6	1
1.4	1.4	1
1.5	1.5	1
1.4	1.4	1
4.7	4.7	0
4.5	4.5	0
4.9	4.9	0
4.0	4.0	0
4.6	4.6	0
(...)		

# Evolution of the academic influence of connexionist and symbolic approaches<sup>1</sup>



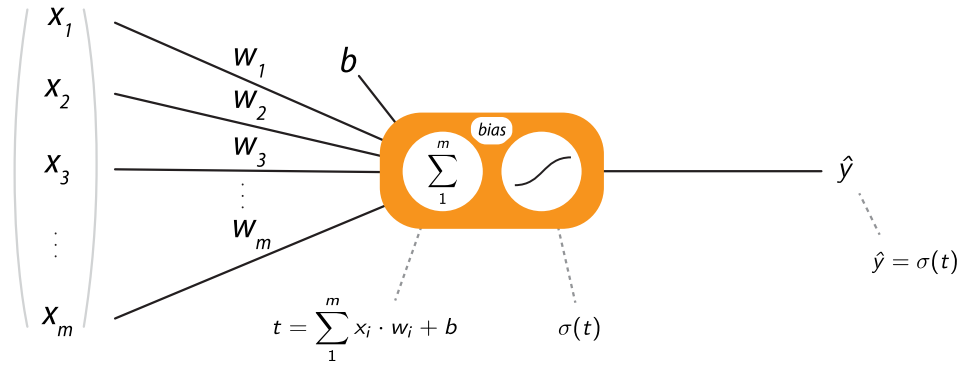
<sup>1</sup> D Cardon, JP Cointet, A Mazieres, 2018 [LRDN]

# Evolution of the academic influence of connexionist and symbolic approaches<sup>1</sup>

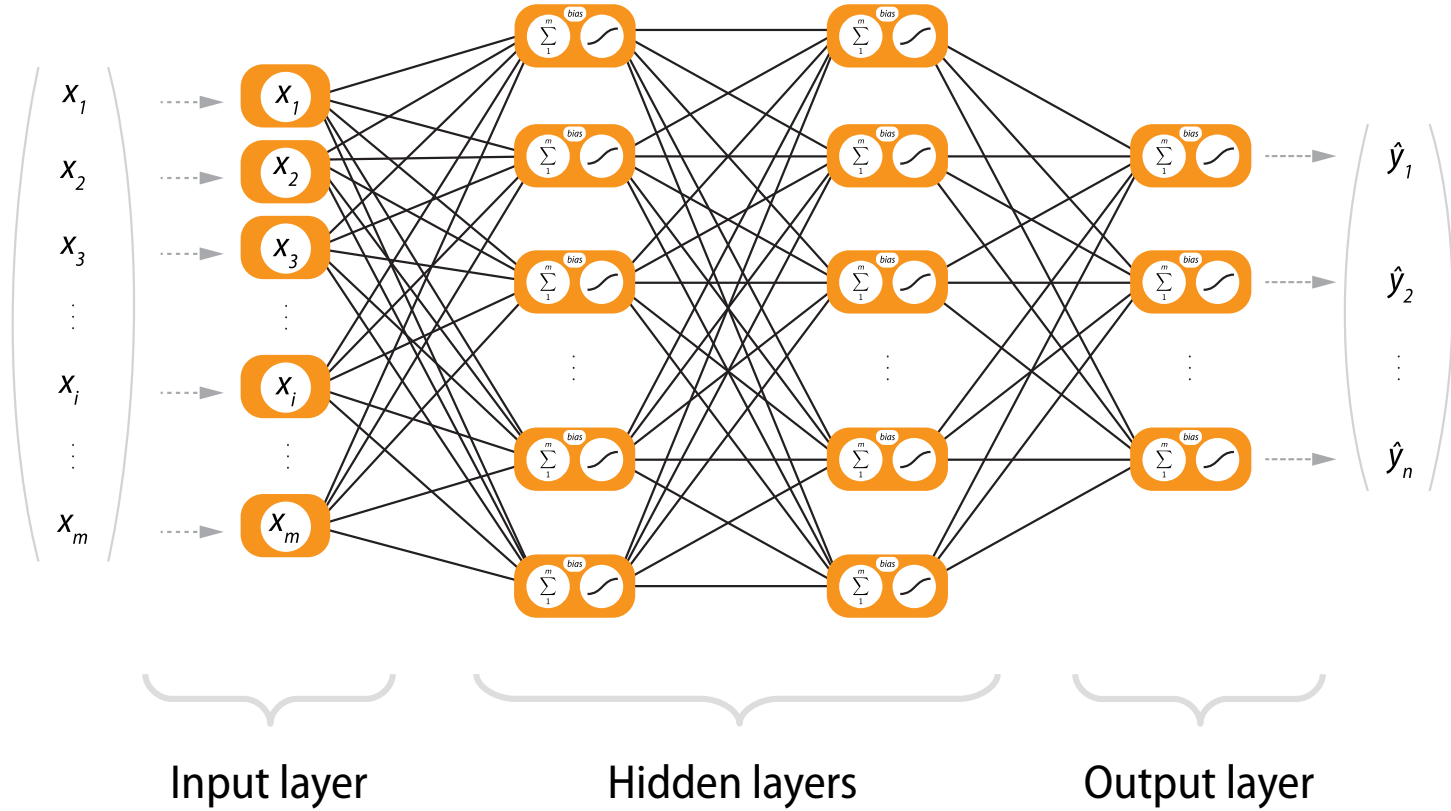


<sup>1</sup> D Cardon, JP Cointet, A Mazieres, 2018 [LRDN]

# Deep Neural Networks

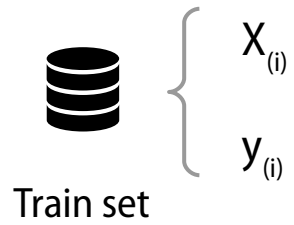


# Deep Neural Networks

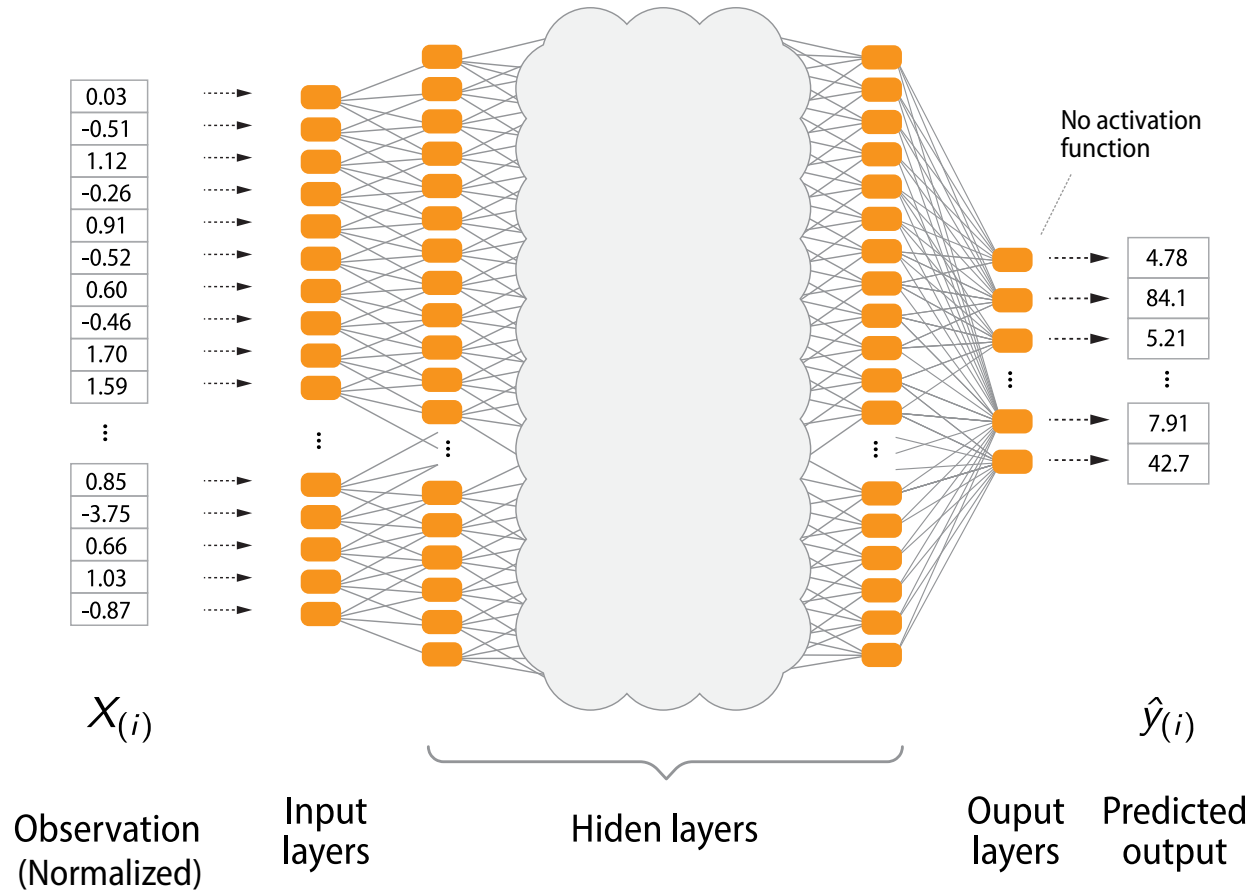




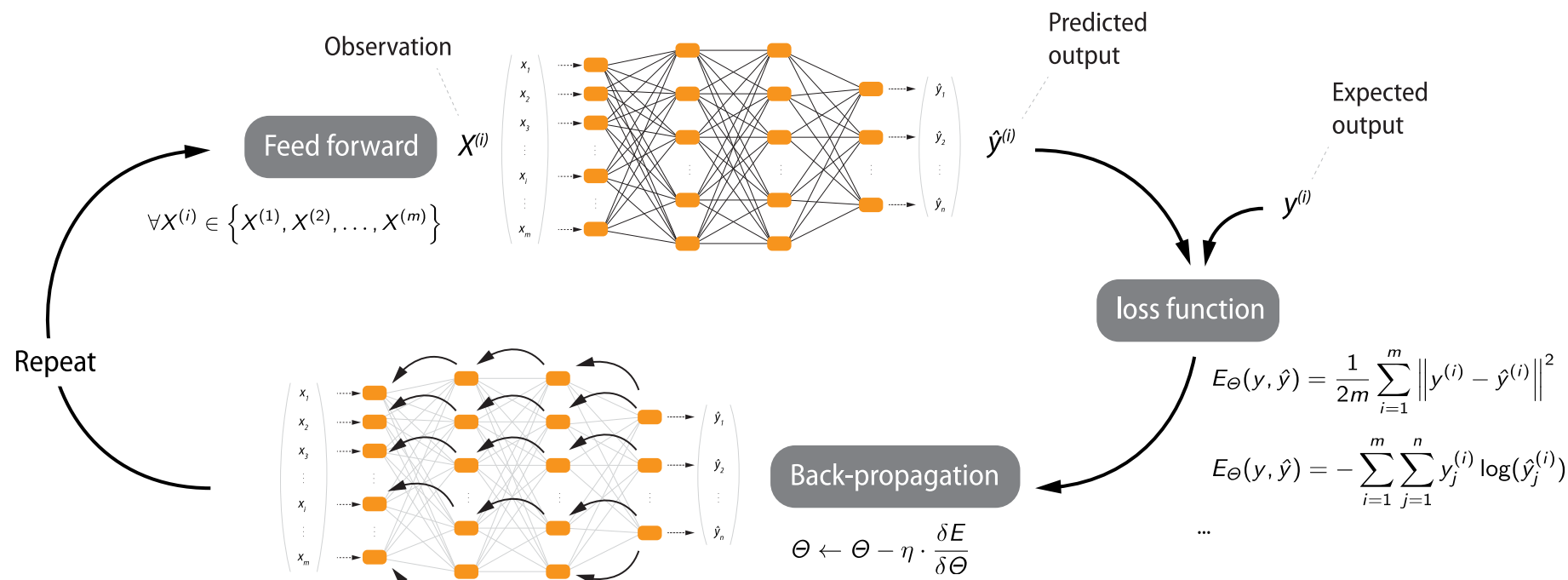
# Deep Neural Networks



$X_{(i)}$  : Observations  
 $y_{(i)}$  : Expected output



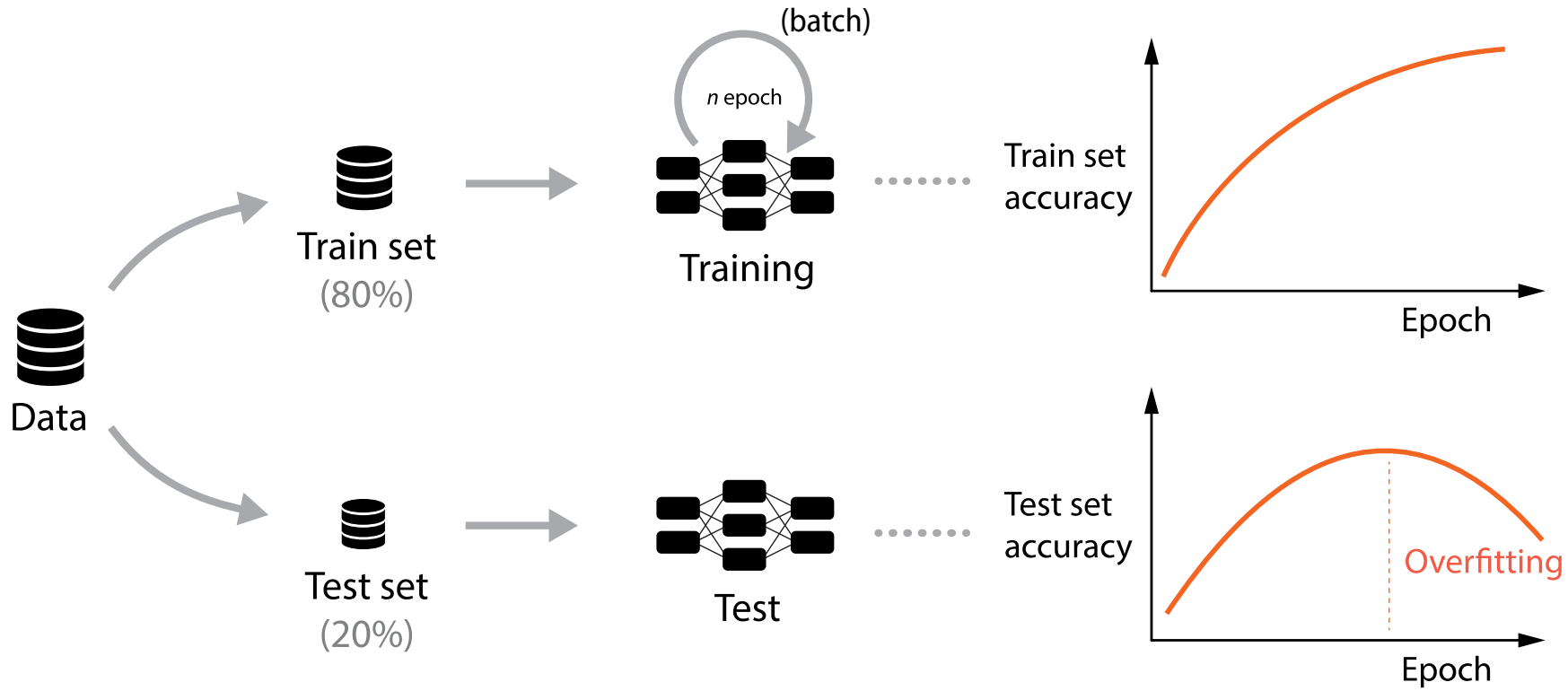
# Deep Neural Networks



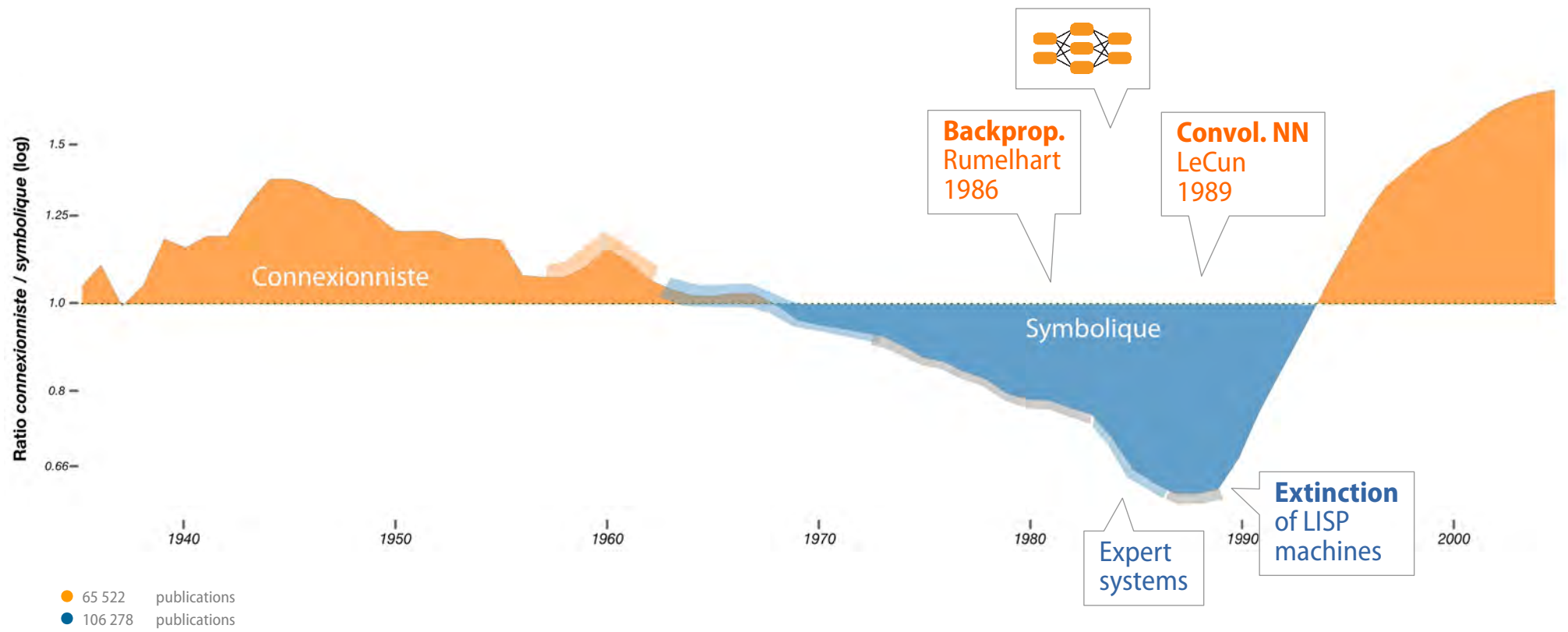
Back-propagation  
Learning process

To define :  
Optimization  
Activation  
Loss  
Metrics  
...

# Training process - general

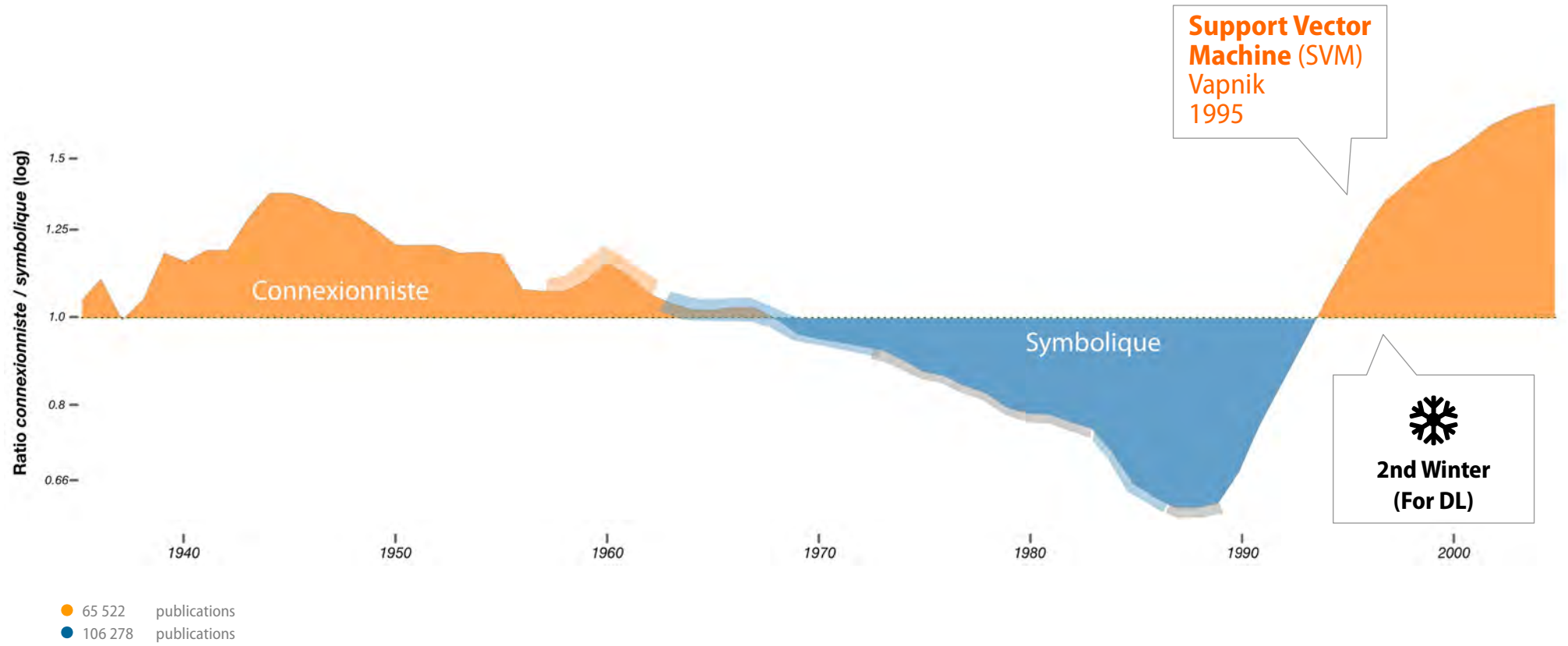


# Evolution of the academic influence of connexionist and symbolic approaches<sup>1</sup>



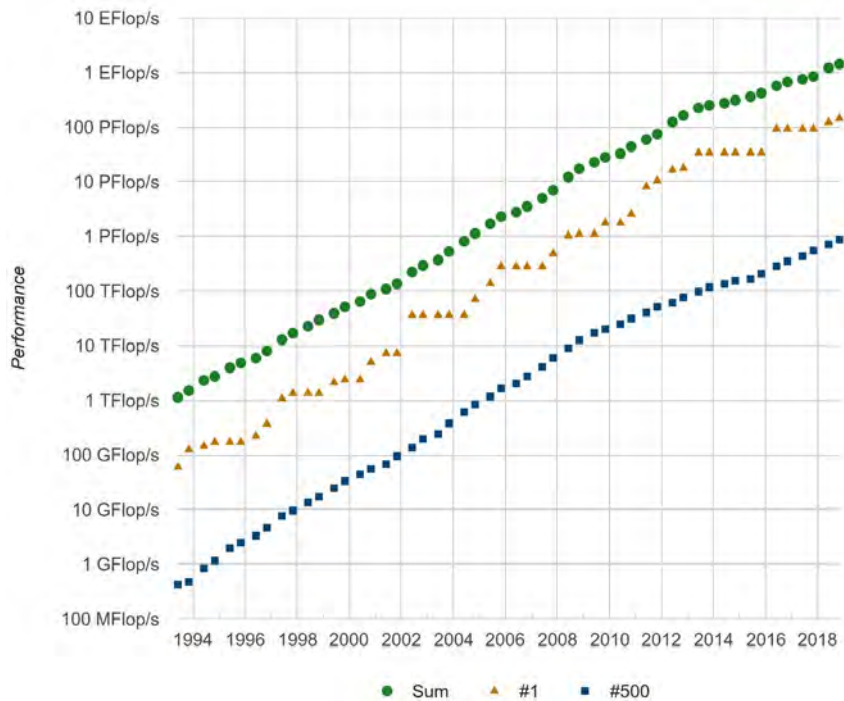
<sup>1</sup> D Cardon, JP Cointet, A Mazieres, 2018 [LRDN]

# Evolution of the academic influence of connexionist and symbolic approaches<sup>1</sup>

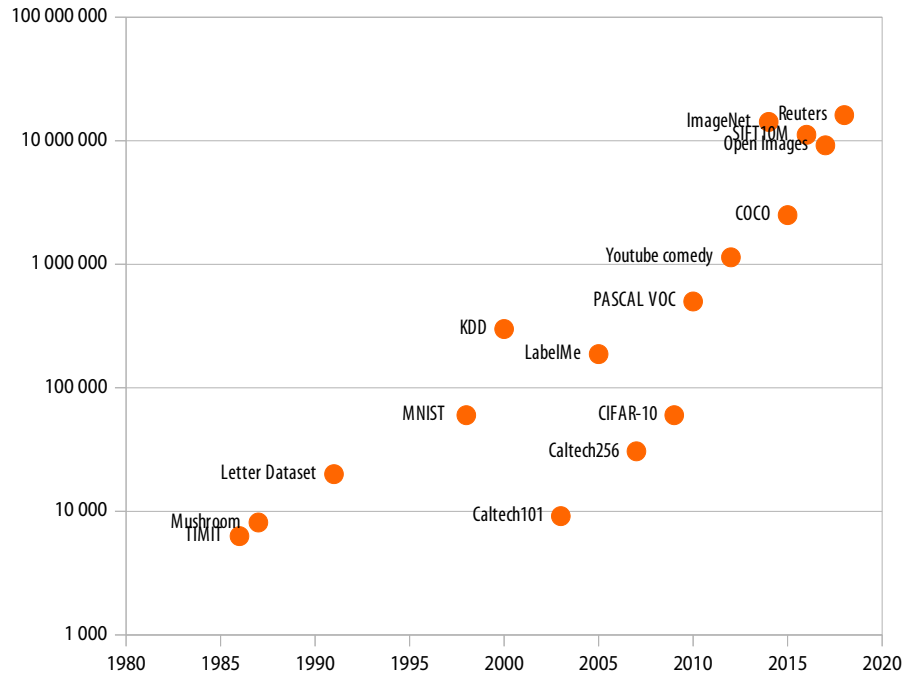


<sup>1</sup> D Cardon, JP Cointet, A Mazieres, 2018 [LRDN]

## Performance Development<sup>1</sup>

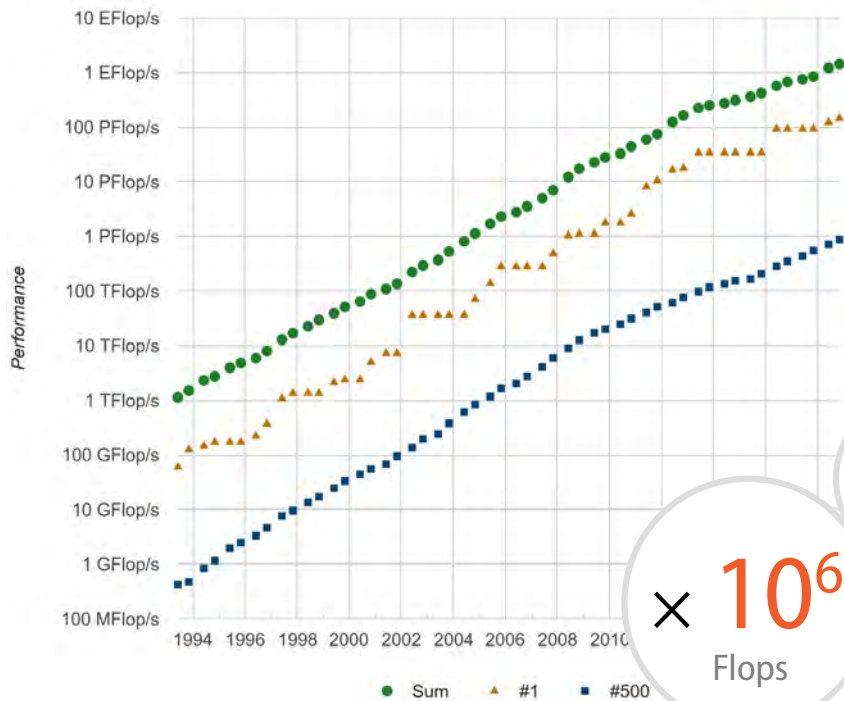


## Datasets for machine-learning<sup>2</sup>



<sup>1</sup> TOP500 List [TOP500] <sup>2</sup> Wikipedia [WKP1]

## Performance Development<sup>1</sup>

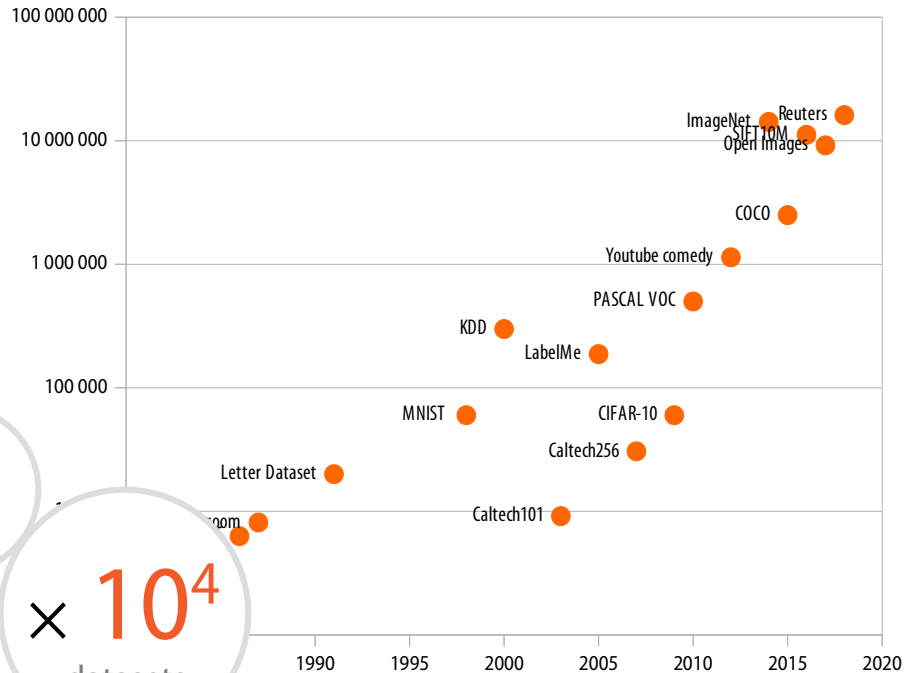


× 10<sup>6</sup>  
Flops

25  
ans

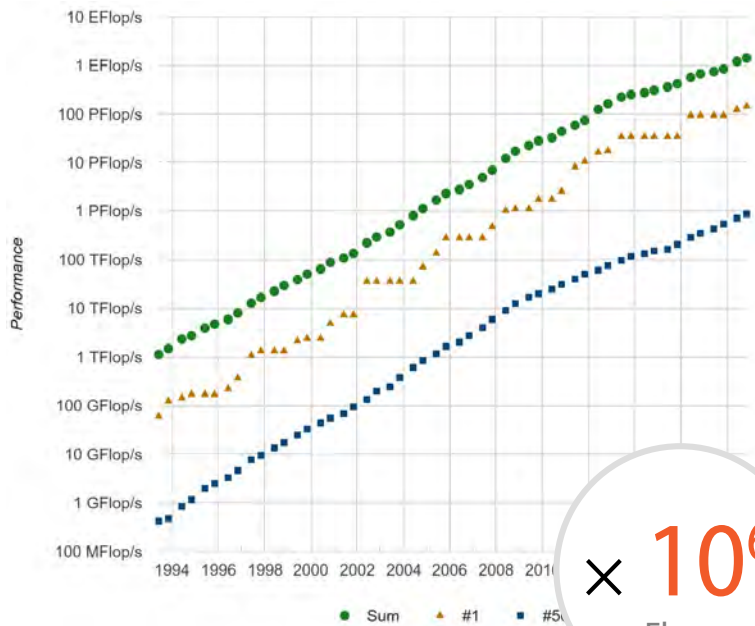
× 10<sup>4</sup>  
datasets

## Datasets for machine-learning<sup>2</sup>



<sup>1</sup> TOP500 List [TOP500] <sup>2</sup> Wikipedia [WKP1]

## Performance Development<sup>1</sup>



×  $10^6$   
Flops

25  
ans

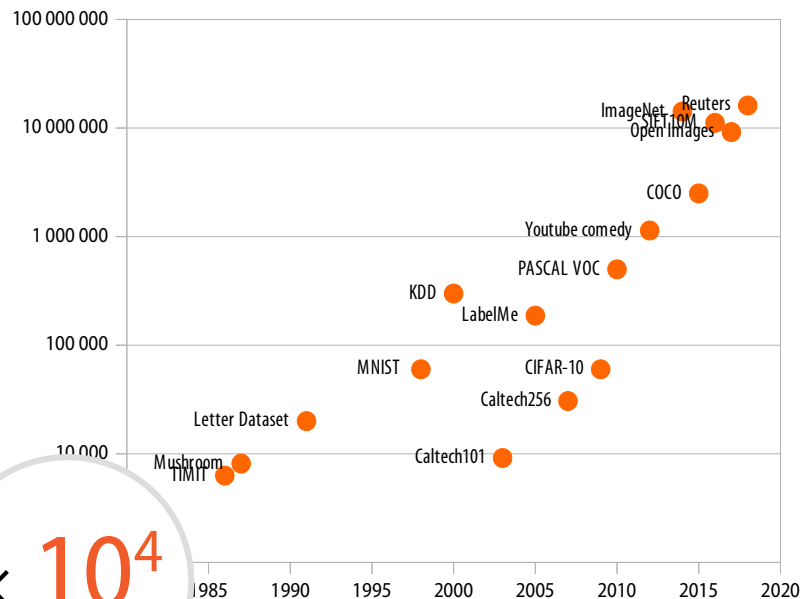
×  $10^4$   
datasets

Laboratory  
Special case



Real world  
High complexity

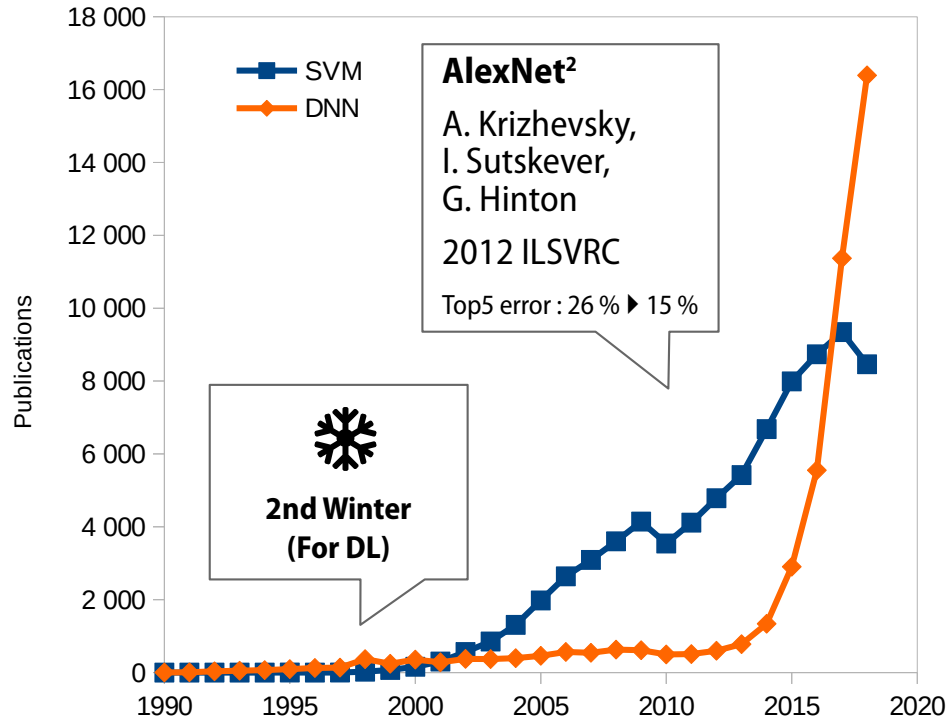
## Datasets for machine-learning<sup>2</sup>



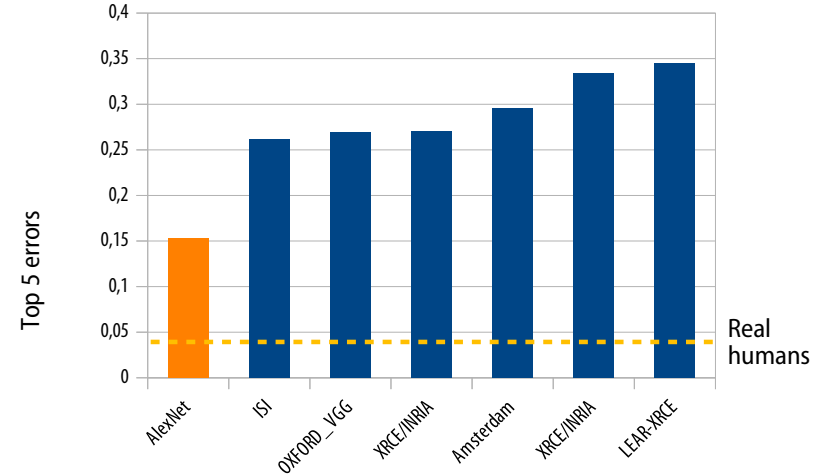
<sup>1</sup> TOP500 List [TOP500] <sup>2</sup> Wikipedia [WKP1]



## Publications SVM vs DNN<sup>1</sup>



## Images classification Top 5 error at ILSVRC 2012<sup>3,4</sup>



Without mathematical guarantee,  
 DNN have proven to be more  
 effective in the face of the  
**complexity of the real world !**

<sup>1</sup> Web of Science [WOS1][WOS2]

<sup>2</sup> AlexNet [ALEX]

<sup>3</sup> ImageNet Large Scale Visual Recognition [ILSVRC]

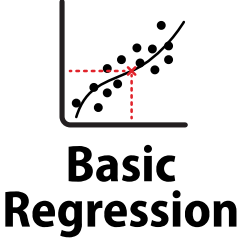
<sup>4</sup> Similar evolution in Natural language processing, translation, board games, etc.  
 See : DeepL.com, AlphaGo, AlphaZero, ...

**3** Neurons at work !



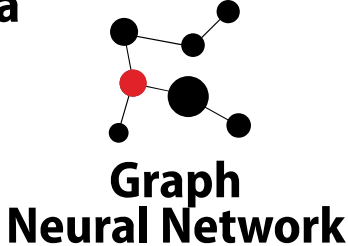
**Hight Dimensional Data**

CNN



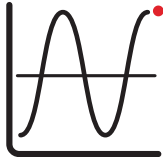
**Basic Regression**

DNN



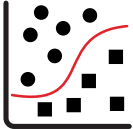
**Graph Neural Network**

GNN



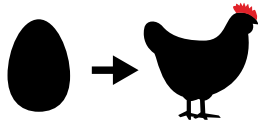
**Sequences data**

RNN



**Basic Classification**

DNN

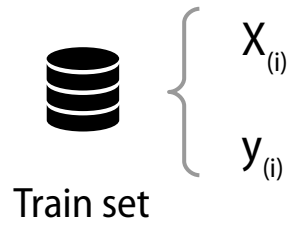


**«Attention is All You Need»**

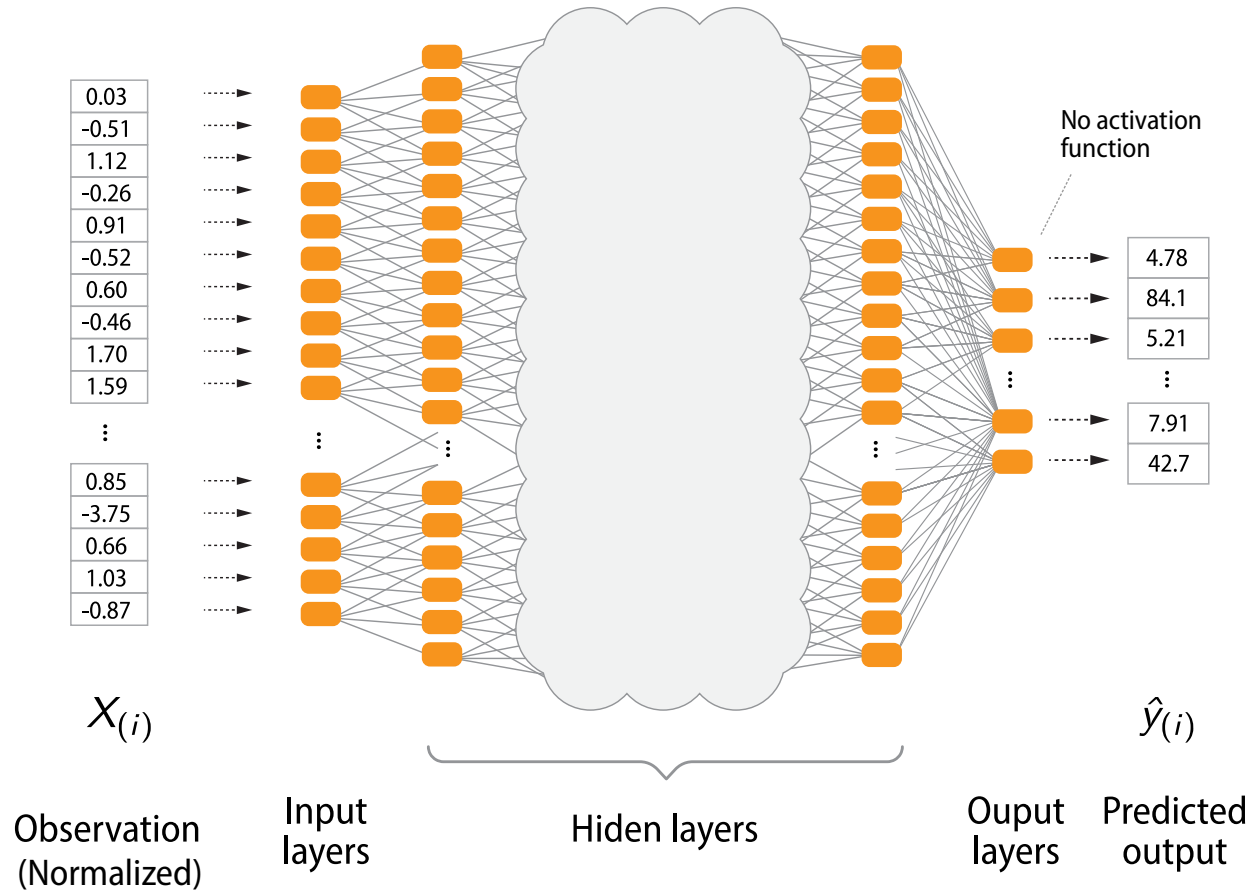
Transformers

...

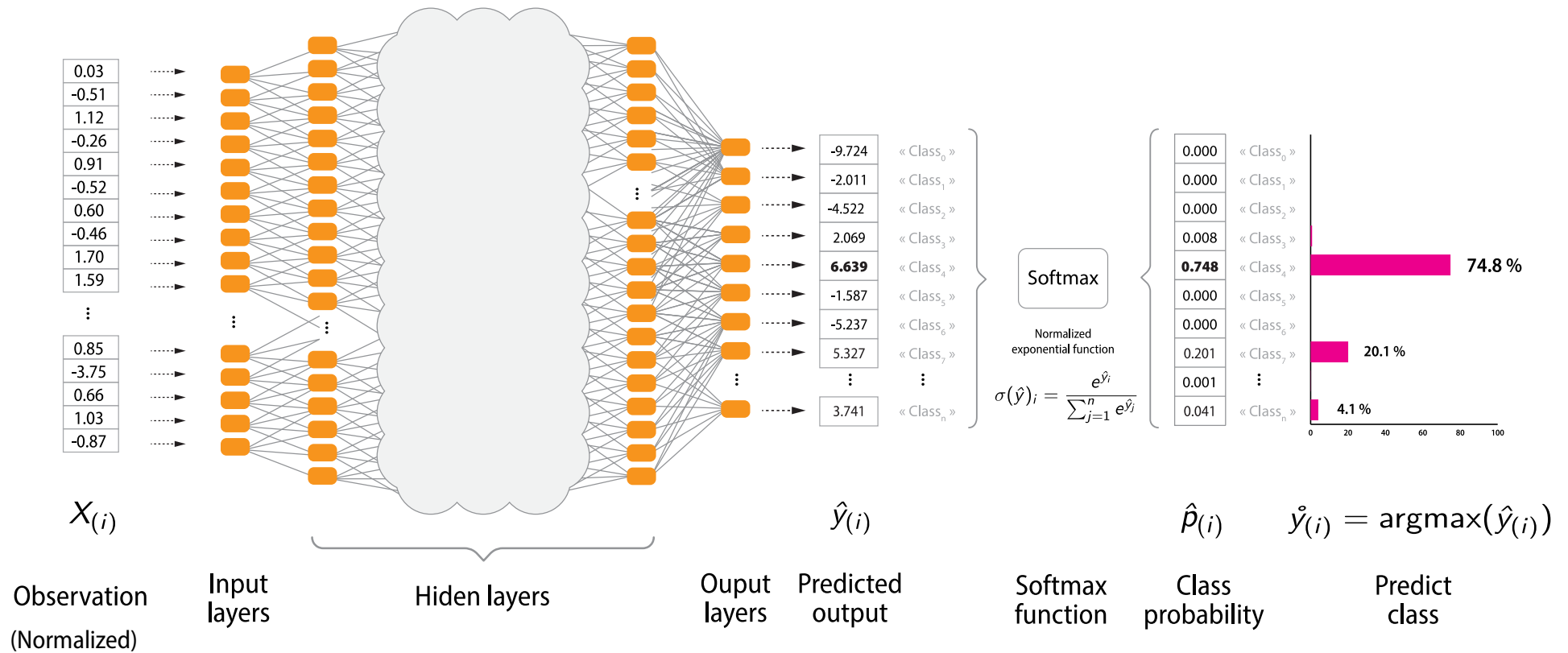
# Regression with a DNN



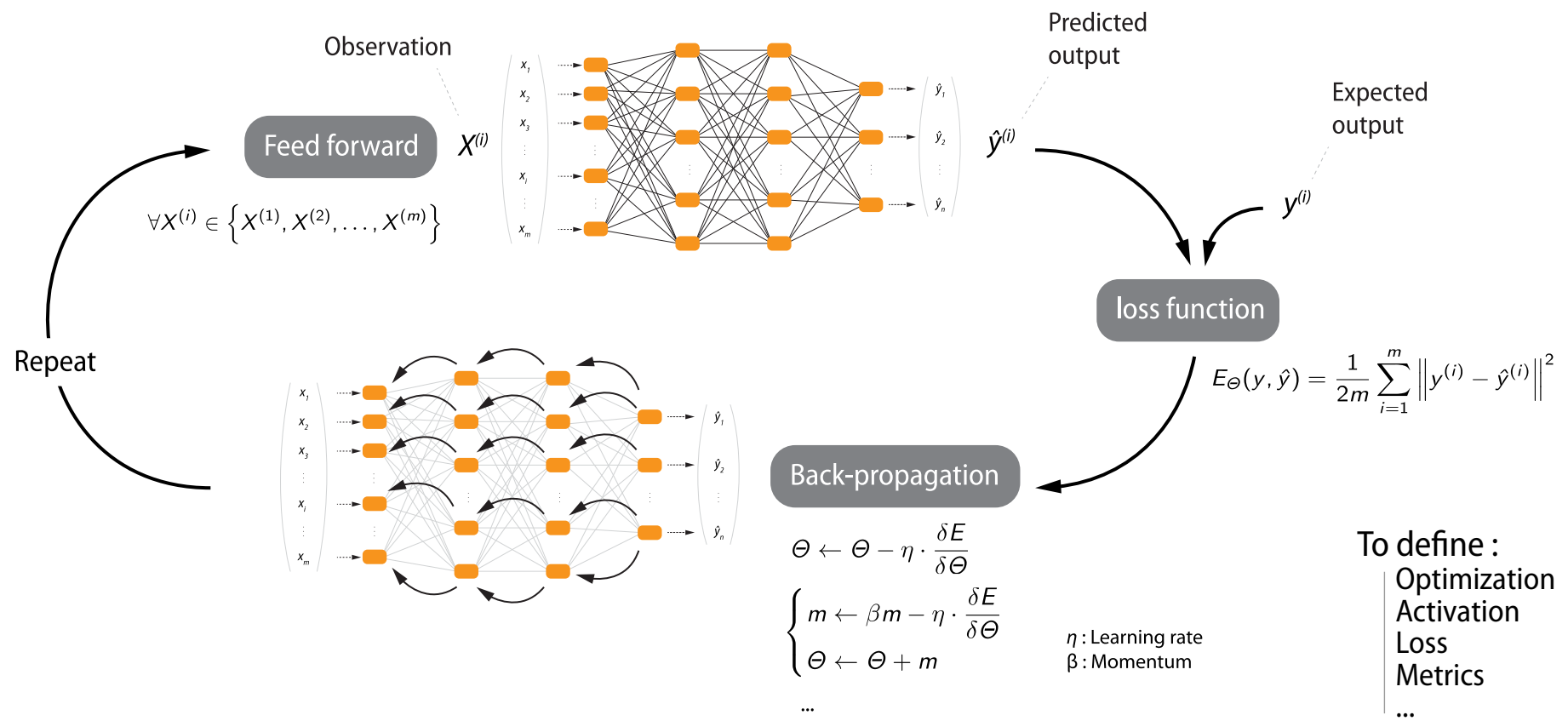
$X_{(i)}$  : Observations  
 $y_{(i)}$  : Expected output



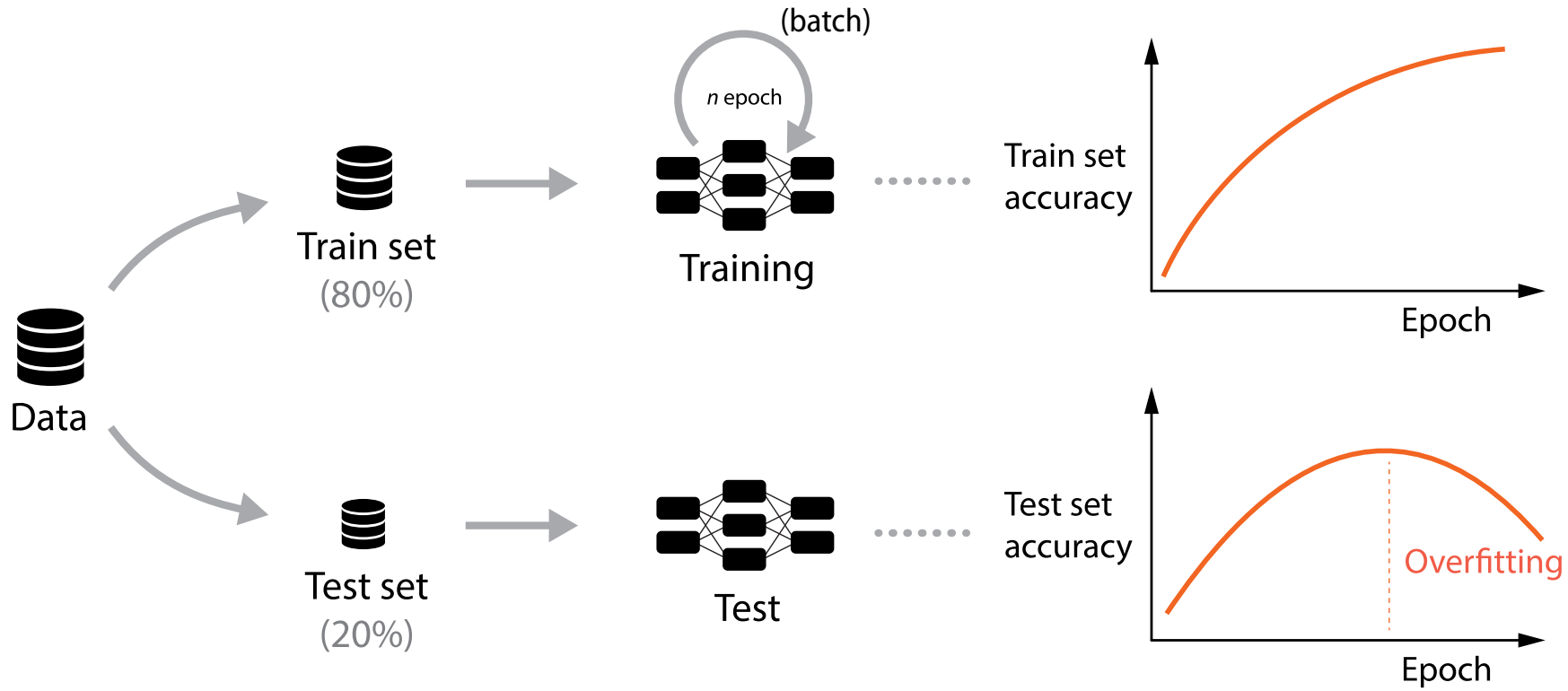
# Classification with a DNN



# Training process - general



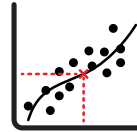
# Training process - general





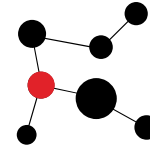
**Hight  
Dimensional Data**

CNN



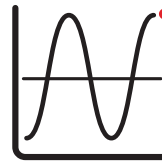
**Basic  
Regression**

DNN



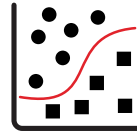
**Graph  
Neural Network**

GNN



**Sequences data**

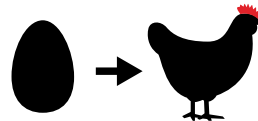
RNN



**Basic  
Classification**

DNN

...

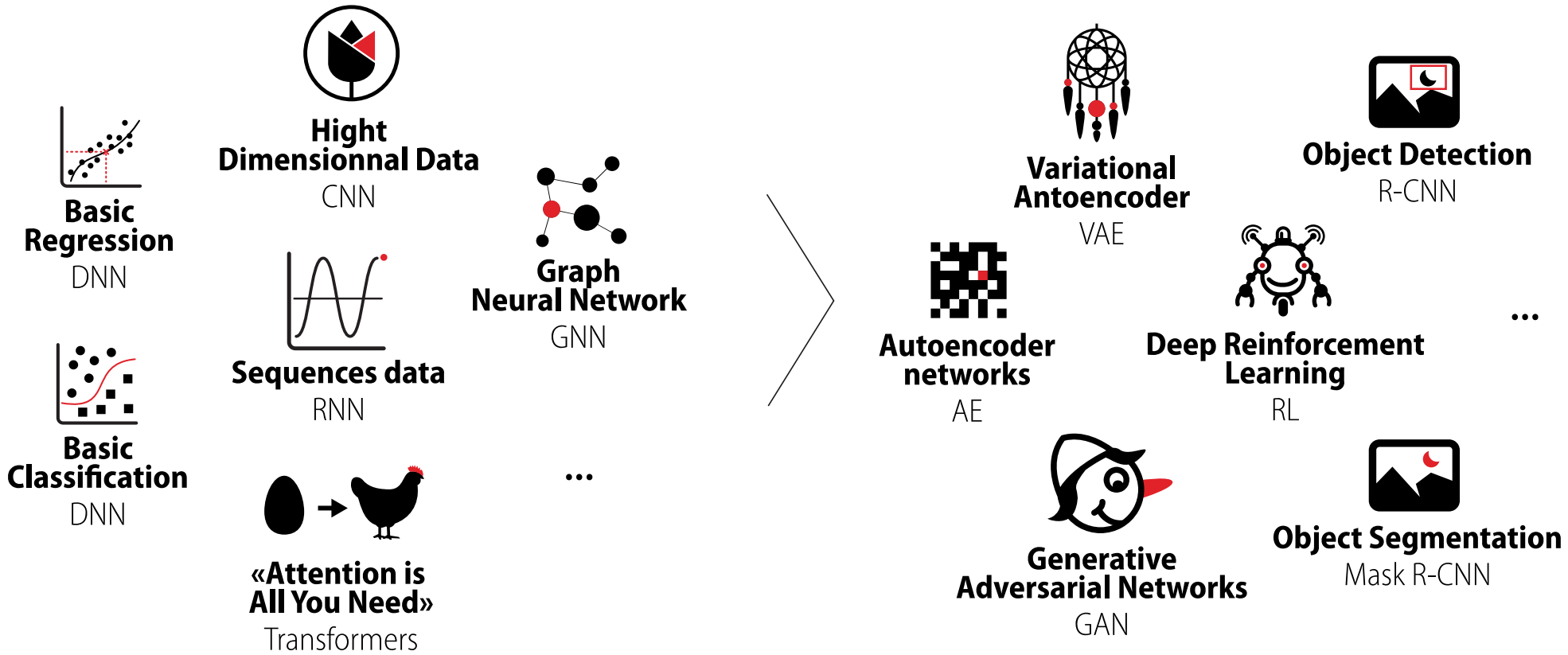


**«Attention is  
All You Need»**

Transformers

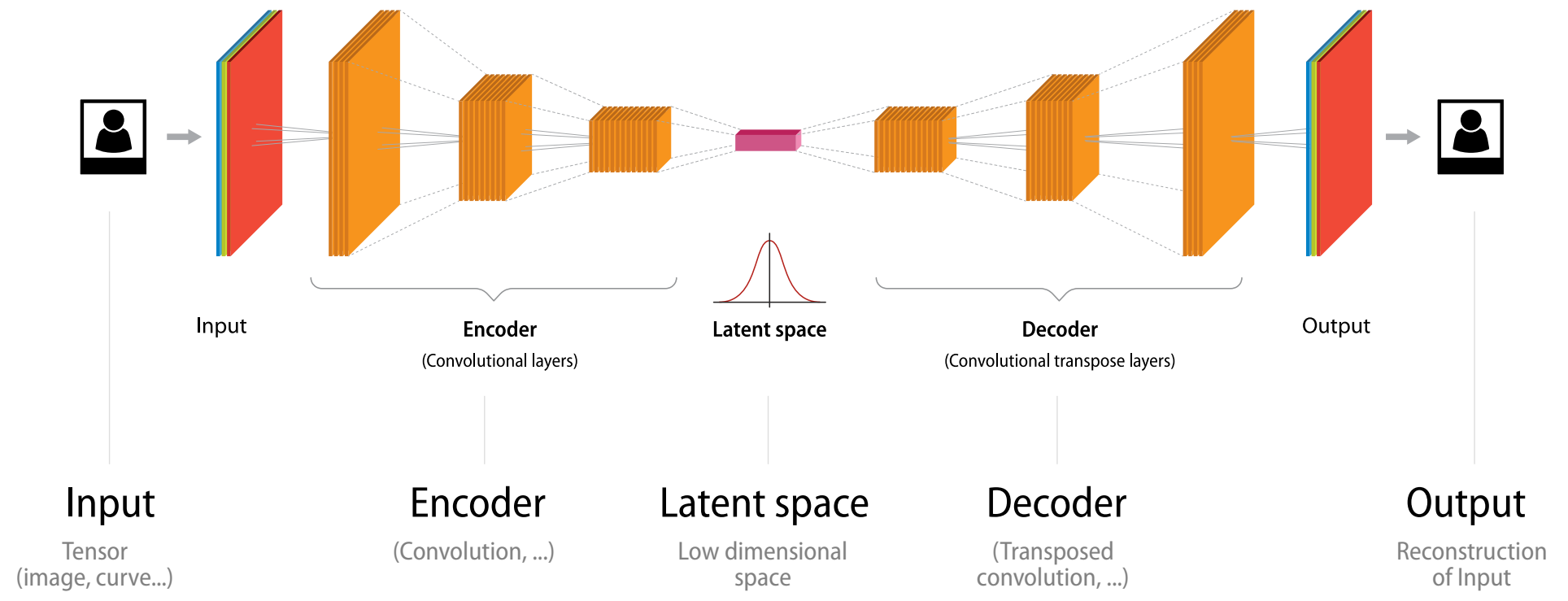


# Neurons and data



# Variational Autoencoder network (VAE)

Autoencoders are trained to minimise reconstruction errors.

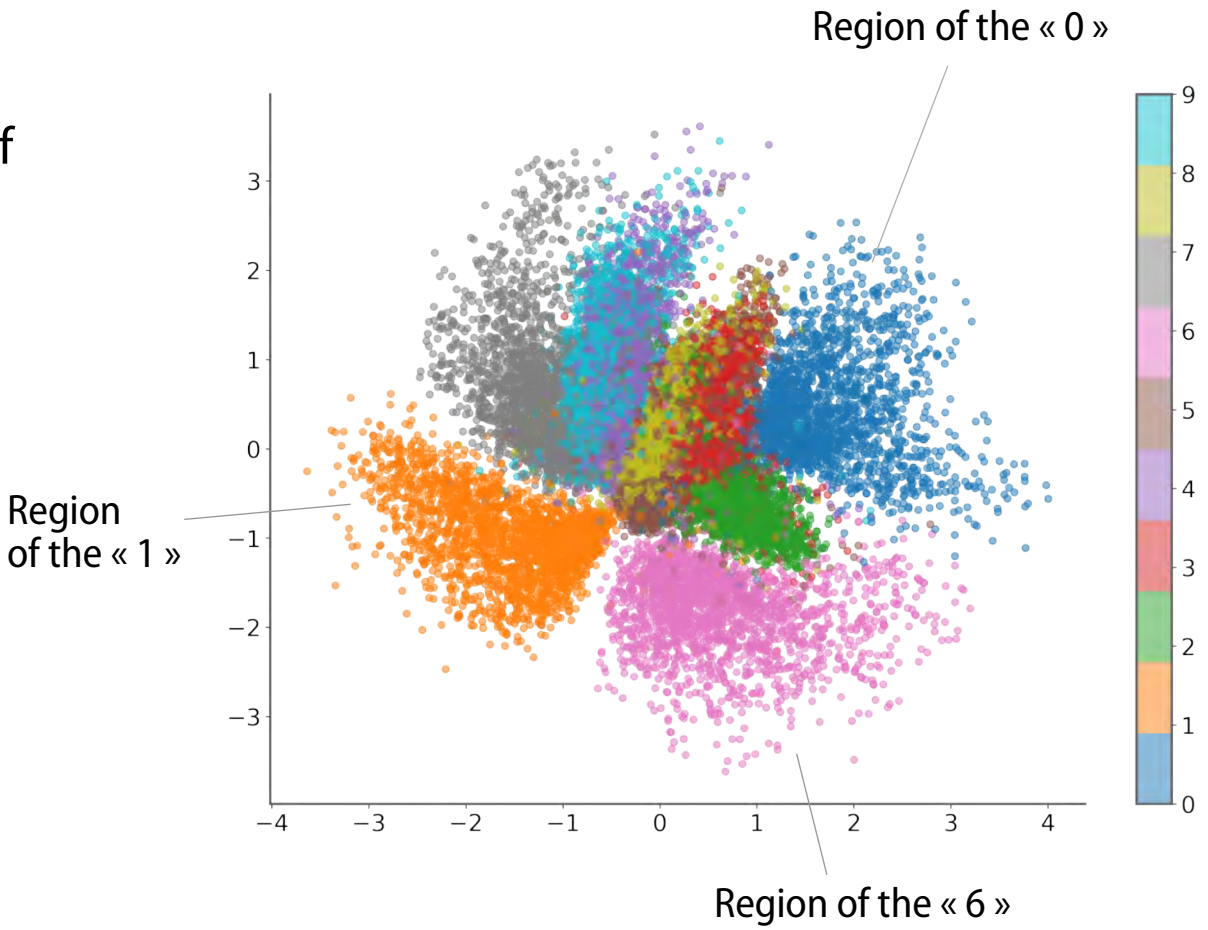
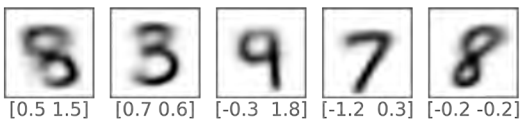


Note : Encoder/Decoder can use convolutional layers or anything else ;-)

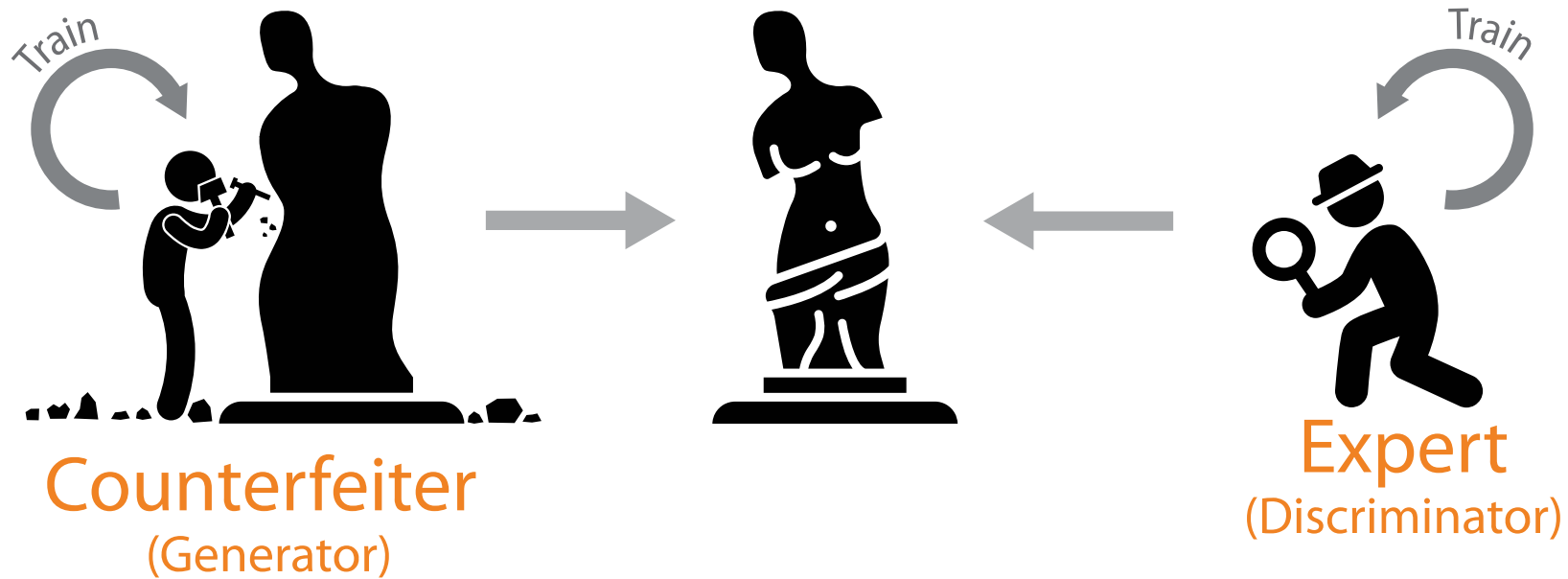
# Variational Autoencoder network (VAE)

Projection of the MNIST dataset into a latent space of dimension 2:

Generate images from latent space:



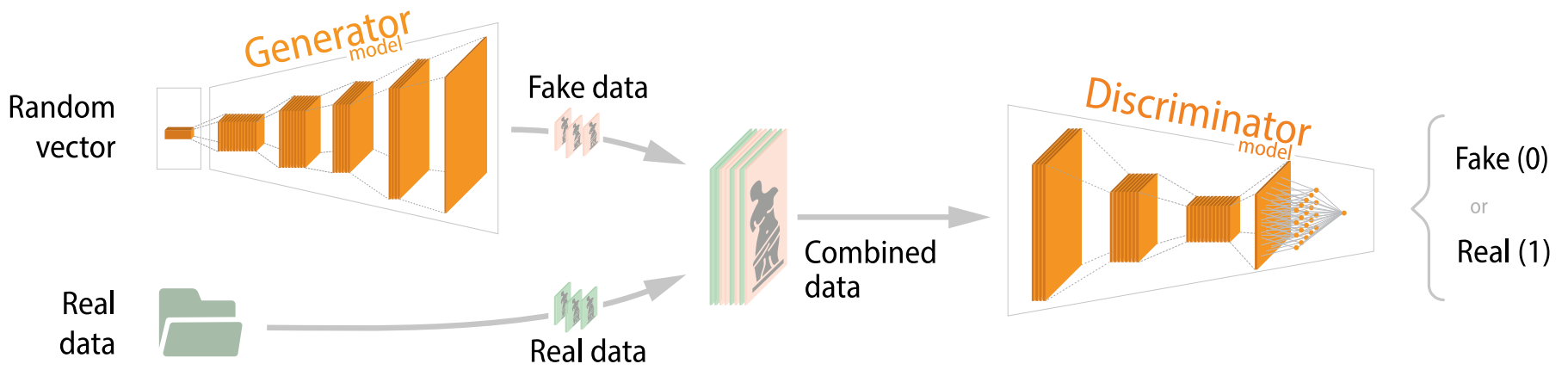
# About GAN



Ian J. Goodfellow, Jean Pouget-Abadie, Mehdi Mirza, Bing Xu, David Warde-Farley, Sherjil Ozair, Aaron Courville et Yoshua Bengio, « Generative Adversarial Networks », in Advances in Neural Information Processing Systems 27, 2014

<https://arxiv.org/abs/1406.2661>

# Principle



## Conditional GANs

Mehdi Mirza, Simon Osindero,  
« Conditional Generative Adversarial Nets »,  
<https://arxiv.org/abs/1411.1784>, 2014



## Progressive GANs

Tero Karras, Timo Aila, Samuli Laine, Jaakko Lehtinen, « Progressive Growing of GANs for Improved Quality, Stability, and Variation »,  
<https://arxiv.org/abs/1710.10196>, 2017



## Image-to-Image Translation

Phillip Isola, Jun-Yan Zhu, Tinghui Zhou, Alexei A. Efros,  
« Image-to-Image Translation with Conditional Adversarial Networks »,  
<https://arxiv.org/abs/1611.07004>, 2016



## CycleGAN

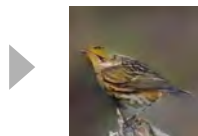
Jun-Yan Zhu, Taesung Park, Phillip Isola, Alexei A. Efros,  
« Unpaired Image-to-Image Translation using Cycle-Consistent Adversarial Networks »,  
<https://arxiv.org/abs/1703.10593>, 2017



## Text-to-Image Synthesis

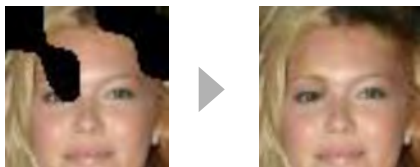
Han Zhang, Tao Xu, Hongsheng Li, Shaoting Zhang, Xiaogang Wang, Xiaolei Huang, Dimitris Metaxas, « StackGAN: Text to Photo-realistic Image Synthesis with Stacked Generative Adversarial Networks », <https://arxiv.org/abs/1612.03242>, 2016

« This smaller brown bird has white stripes on the coverts, wingbars and secondaries »



## Semantic Image Inpainting

Raymond A. Yeh, Chen Chen, Teck Yian Lim, Alexander G. Schwing, Mark Hasegawa-Johnson, Minh N. Do, « Semantic Image Inpainting with Deep Generative Models », <https://arxiv.org/abs/1607.07539>, 2016



## Super-Resolution

Christian Ledig, Lucas Theis, Ferenc Huszar, Jose Caballero, Andrew Cunningham, Alejandro Acosta, Andrew Aitken, Alykhan Tejani, Johannes Totz, Zehan Wang, Wenzhe Shi, « Photo-Realistic Single Image Super-Resolution Using a Generative Adversarial Network », <https://arxiv.org/abs/1609.04802>, 2016

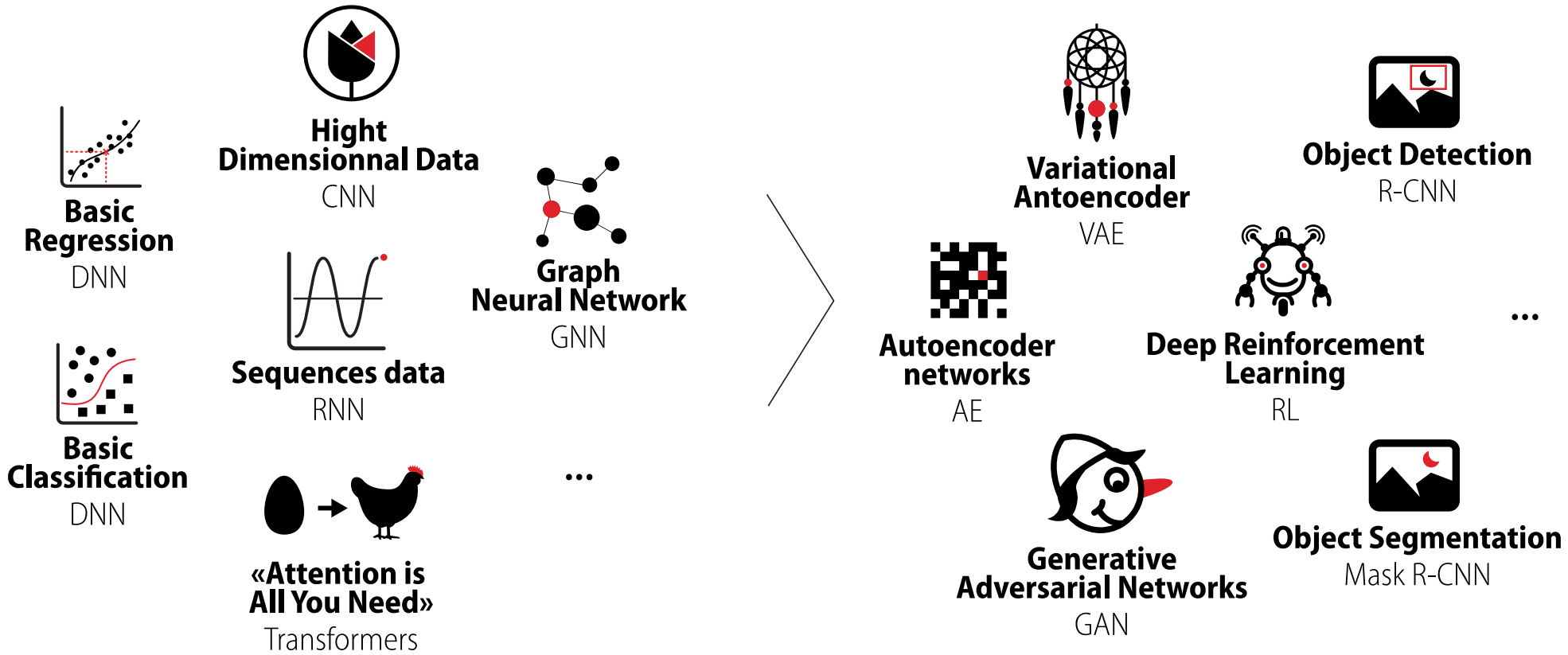


## Face Frontal View Generation

Rui Huang, Shu Zhang, Tianyu Li, Ran He, « Beyond Face Rotation: Global and Local Perception GAN for Photorealistic and Identity Preserving Frontal View Synthesis », <https://arxiv.org/abs/1704.04086>, 2017

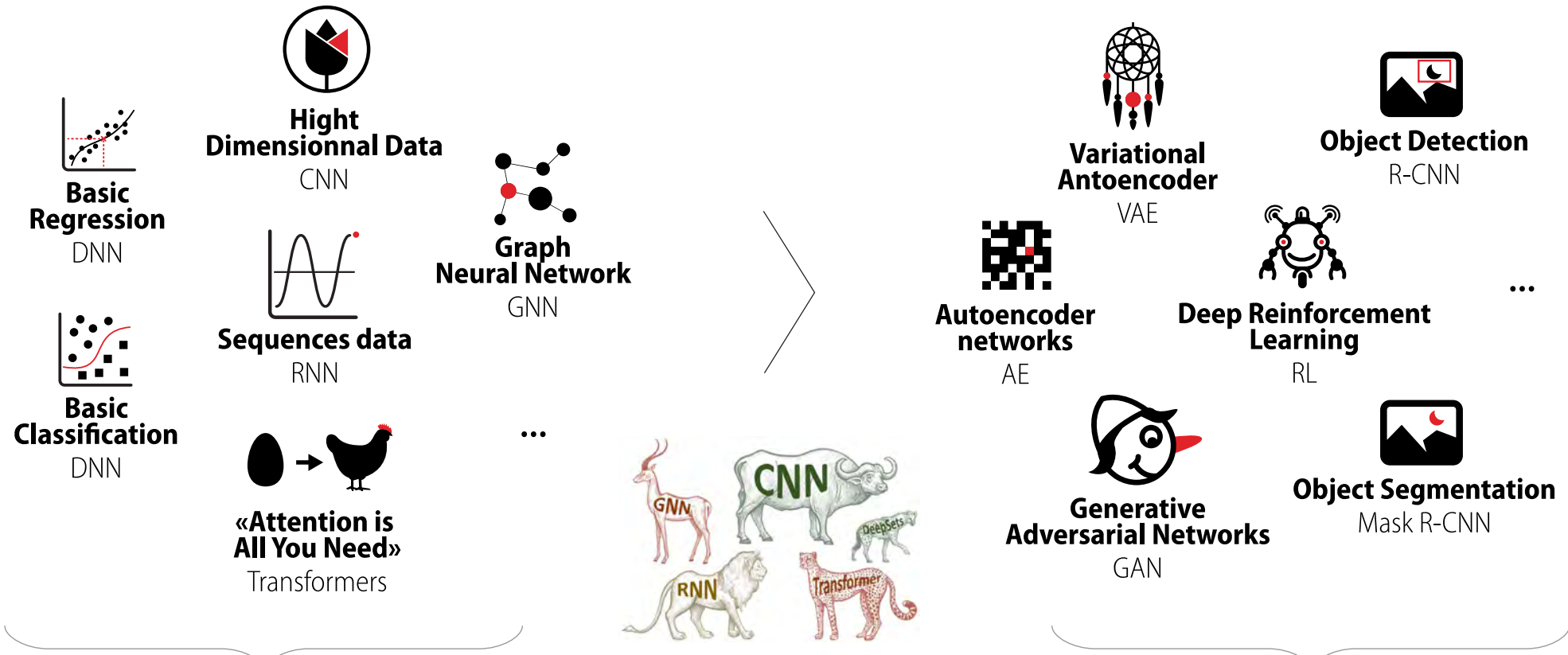


# Neurons and data





# Neurons and data



«Zoo of neural network architectures for different kinds of data»

## Geometric Deep Learning ?

BRONSTEIN, Michael M., BRUNA, Joan, COHEN, Taco, et al. Geometric deep learning: Grids, groups, graphs, geodesics, and gauges. arXiv preprint arXiv:2104.13478, 2021.a

## Pipelines

- For a slightly longer version -



Formation  
Introduction au  
**Deep Learning**

<https://fidle.cnrs.fr>

Merci !



 [Contact@fidle.cnrs.fr](mailto:Contact@fidle.cnrs.fr)  
 FIDLE <https://fidle.cnrs.fr>  
 YouTube <https://fidle.cnrs.fr/youtube>



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# Références

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ISBN: 978-0-9825442-0-4
- [FROS] Rosenblatt, Frank. (1958). « The perceptron: A probabilistic model for information storage and organization in the brain. » *Psychological Review*, 65(6), 386-408.
- [MIPA] Minsky, Marvin; Papert, Seymour. (1969). « Perceptrons : An Introduction to Computational Geometry », MIT Press
- [DRUM] Rumelhart, David E.; Hinton, Geoffrey E.; Williams, Ronald J. (1986). « Learning representations by back-propagating errors ». *Nature*. 323 (6088): 533–536. doi:10.1038/323533a0.
- [YLEC1] Y. LeCun, B. Boser, J. S. Denker, D. Henderson, R. E. Howard, W. Hubbard, L. D. Jackel, « Backpropagation Applied to Handwritten Zip Code Recognition », AT&T Bell Laboratories
- [LRDN] Dominique Cardon, Jean-Philippe Cointet, Antoine Mazieres. (2018). « La revanche des neurones », *Réseaux, La Découverte*, 5 (211), <10.3917/res.211.0173>. <hal-01925644>
- [TOP500] Statistics on top 500 high-performance computers. (2018) « Exponential growth of supercomputing power as recorded by the TOP500 list ». <https://www.top500.org>
- [WKP1] Wikipedia/en. (2018) « List of datasets for machine-learning research ». <https://en.wikipedia.org>
- [WOS1] Core database : TS=("support vector machine\*" OR ("SVM" AND "classification") OR ("SVM" AND "regression") OR ("SVM" AND "classifier") OR "support vector network\*" OR ("SVM" AND "kernel trick\*"))
- [WOS2] Core database : TS=("deep learning" OR "deep neural network\*" OR ("DNN" AND "neural network\*") OR "convolutional neural network\*" OR ("CNN" AND "neural network\*") OR "recurrent neural network\*" OR ("LSTM" AND "neural network\*") OR ("RNN\*" AND "neural network\*"))

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Icons [thenounproject.com](https://www.thenounproject.com)